

Classwork 18.



1. Represent the monomials as a square of another monomials:

Example:

$$\frac{1}{4}a^6x^8 = \left(\frac{1}{2}a^3x^4\right)^2;$$

a. $25a^3$;

b. $16c^4$;

c. $2\frac{1}{4}a^{10}x^6$;

d. $64k^8$;

e. $\frac{1}{49}p^8$;

f. $2\frac{7}{9}b^{12}y^{10}$;

2. Are the transformations carried out correctly:

a. $(2x + 3y)(3x - 2y) = 6x^2 - 4xy + 9xy - 6y^2 = 6x^2 + 5xy - 6y^2$;

b. $(xy^2 + x^2y)(xy + 3) = x^2y^3 + 3xy^2 + x^3y^2 + 3x^2y$

3. Simplify the expressions:

a) $(2x - 2a)(3a^2 - 4a + 5)$; b) $(7x^2 - 2x + 4 - x^2)(2x - x - 1)$;

c) $(x^2 + 3x - 2)(2x^2 - x + 4)$; d) $(2m^3 - 7m^2 + 4m)(3 - 8m + m^2)$;

e) $(2a + 1)(3 + a)(5a + 2)$; f) $(x - 3)(2x - 1)(7 + 2x)$

g) $(2m - n)(3n + 2m)(m - 5n)$; h) $(p - 8q)(4q - p)(p + 8q)$.

4. Determine whether the polynomial is a square of any binomial.

a. $a^2 + 4ac + 4c^2$;

b. $1 + x^2 + 2x$;

c. $a^2c^2 + 2acd + d^2$;

d. $9 + 5x + x^2$

e. $a^2 - 2ab + b^2$;

f. $1 + 9x^2 - 6x$;

g. $x^4 - 6x^2y + 9y^2$;

h. $25 - 30c + 9c^2$

5. Simplify the expression using the formula for the difference of squares. First rewrite the expression as a difference of squares, then simplify the exponent notation.

Example:

$$(3a - 2b)(3a + 2b) = (3a)^2 - (2b)^2 = 9a^2 - 4b^2;$$

$$(x + 2y)(x - 2y);$$

$$(3m - n)(3m + n);$$

$$(2a - 3b)(2a + 3b);$$

$$(4p - 1)(1 + 4p);$$

$$(4y - 7x)(7x + 4y);$$

$$(2a + b)(2a - b);$$

$$(p - 7q)(7q + p);$$

$$(5x + 4y)(4y - 5x);$$

$$(5m + 8n)(8n - 5m);$$

$$(11a - 13b)(11a + 13b).$$

6. Factor the polynomial:

$$y^2 - x^2;$$

$$9 - (3m)^2;$$

$$25 - a^6;$$

$$p^8 - 49;$$

$$a^4 - b^4.$$

$$a^2 - b^2;$$

$$(2x)^2 - 1;$$

$$16 - p^4;$$

$$m^4 - n^2;$$

$$1 - x^4;$$

7. Completing the square:

$$a^2 + 8a + 15;$$

$$m^2 + 7m + 10;$$

$$x^2 + x - 12;$$

$$x^4 + 4b^4;$$

$$p^2 - 5p + 6;$$

$$a^2 + 6a + 8;$$

$$x^2 - 2xy - 3y^2;$$

$$3m^2 + 27m + 54;$$

$$x^2 - x - 12.$$