Math 6, SchoolNova Homework 9

(1) We take the standard card deck and draw one card. What is the probability that the card will be

- (a) Queen of hearts
- (b) Either a queen or a hearts card
- (c) A red card
- (d) A picture card (a jack, queen, king, ace)
- (e) A picture card other than the queen of hearts
- (2) (a) What is the probability that when we toss a coin 4 times, there will be no heads?
  - (b) A and B are playing the following game. They toss a coin 4 times; if there are no heads, A wins, and B pays him \$10. Otherwise A loses and he pays \$1 to B. Would you prefer to play for A or for B in this game?
- (3) (a) What is the probability that when we roll two dice, at least one will be a 6?
  - (b) A and B are playing the following game. They roll two dice; if at least one is a 6, A wins, and B pays him \$5. Otherwise A loses and he pays \$1 to B. Would you prefer to play for A or for B in this game?
- (4) (a) What is the probability that if we roll 3 dice, all the numbers will be odd?
  - (b) A and B are playing the following game. They roll 3 dice; if all numbers are odd, A wins, and B pays him \$5. Otherwise A loses and he pays \$1 to B. Would you prefer to play for A or for B in this game?
- (5) Supposing that there are equal chances of a boy or a girl being born, what is the probability that the first five babies born next Saturday morning at the St. Charles Hospital will be girls? That at least one of them five will be a girl?

(6)	In a certain club of 30 people, they are selecting a president, vice-president, and a treasurer (they all must be different people: no one is allowed to take two posts at once). How many ways are there to do this?
(7)	In a group of 100 students, 28 speak Spanish, 30 speak German, 42 speak French; 8 students speak Spanish and German, 10 speak Spanish and French, 5 speak German and French and 3 students speak all 3 languages. How many students do not speak any one of the three languages?
(8)	How many whole numbers between $1-1000$ are divisible by $3?$ $5?$ $15?$ are not divisible by either $3$ or $5?$
(9)	<ul> <li>(a) What is the probability that if we roll 2 dice, the sum will be at most 7?</li> <li>(b) A and B are playing the following game. They roll 2 dice; if the sum is at most 7, A wins, and B pays him \$1. Otherwise A loses and he pays to B \$1.</li> <li>Would you prefer to play for A or for B in this game?</li> </ul>
(10)	<ul> <li>(a) What is the probability that if we roll 3 dice, all the numbers will be different?</li> <li>(b) A and B are playing the following game. They roll 3 dice; if all numbers are different, A wins, and B pays him \$2. Otherwise A loses and he pays to B \$3.</li> <li>Would you prefer to play for A or for B in this game?</li> </ul>
(11)	<ul> <li>(a) In a class of 25 students, everyone chooses a date (e.g., March 13). How many combinations are possible? (Students only choose month and day, not year; February 29th is not allowed, so there are 365 different possibilities. Also, it matters who had chosen which day: combination where Bill has chosen March 12 and John, June 15 is considered different from the one where Bill has chosen June 15 and John March 12.)</li> <li>(b) In the same situation, how many such combinations are possible if we additionally require that all dates must be different?</li> <li>(c) (*) Suppose now that each of these 25 students has chosen a date at random, not knowing the choices of others. What is the probability that all of these dates will be different? That at least 2 will coincide?</li> </ul>