

**Density:**

$$\rho = \frac{Mass}{Volume}$$

Example: density of water  $1000 \frac{kg}{m^3} = 1 \frac{kg}{l} = 1 \frac{g}{cm^3} = 1 \frac{g}{ml}$

$$Pressure = \frac{Force}{Area}$$

**Units of Pressure:**

$$1Pa = 1 \frac{N}{m^2} \text{ (standard SI unit called Pascal)}$$

$$1 bar = 100 kPa = 10^5 Pa$$

Atmospheric Pressure  $1 atm = 101 kPa$ , it is very close to 1 bar.

# Pressure in fluids

- Pascal's Principle:

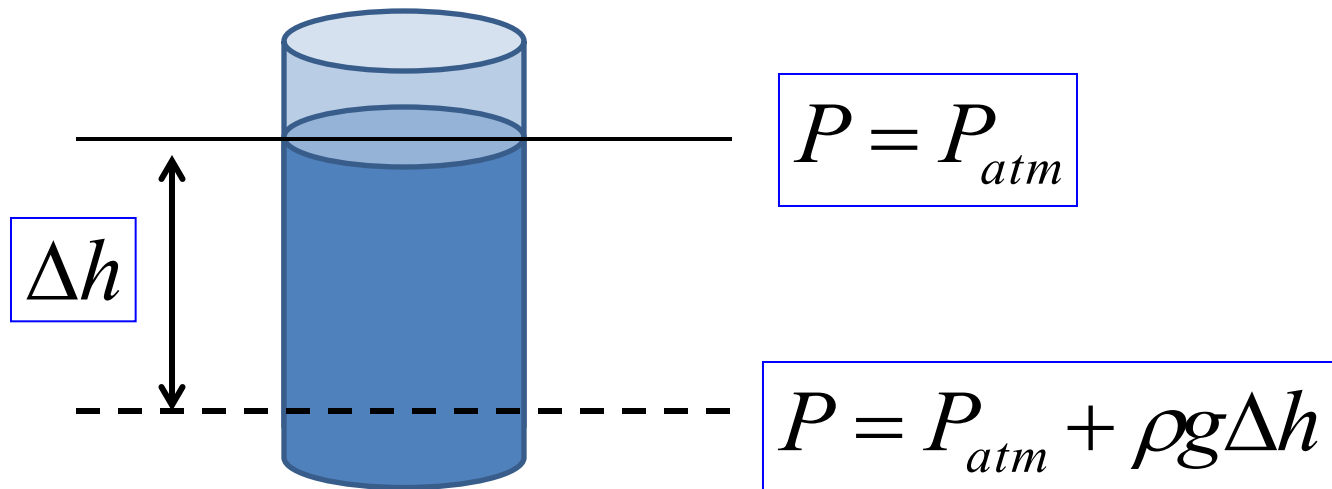
*"Pressure in static fluid is transmitted uniformly in all directions"*

$$P = \text{const}$$

(static fluid, no gravity)

- **Hydrostatic Pressure.** Due to gravity, the pressure increases as you go deeper in fluid:

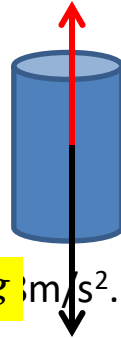
$$\Delta P = \rho g \Delta h$$



# Buoyancy

- Archimedes Principle : ***"Buoyancy force = weight of displaced fluid"***

$$\text{Bouyancy Force} = \rho_{\text{fluid}} V g$$



$$F_{\text{bouyancy}} = m_{\text{fluid}} g = \rho_{\text{fluid}} V g$$

here \ Weight of the body =  $m_{\text{body}} g$  in  $\text{m/s}^2$ .

- Buoyancy also acts on objects in gases (think of balloons in air).
- Units of Volume and Density:

$$1\text{m}^3 = 10^3\text{l} = 10^6\text{cm}^3$$

$$1\text{cm}^3 = 1\text{ml} = 10^{-3}\text{l} = 10^{-6}\text{m}^3$$

$$\rho_{\text{H}_2\text{O}} = 1 \frac{\text{g}}{\text{ml}} = 1000 \frac{\text{kg}}{\text{m}^3}$$

# Homework

## Problem 1

Imagine that you have extremely accurate digital scales that were calibrated in vacuum (in the presence of regular Earth gravity). How much will they show (in grams) if you weight  $m=1\text{kg}$  of Aluminum, in the presence of atmosphere? Density of Aluminum is  $\rho_{\text{Al}}=2.800\text{ kg/m}^3$ , density of air is  $\rho_{\text{air}}=1.2\text{ kg/m}^3$ .

## Problem 2.

Two U-shaped pipes are used to measure pressure in a sealed tank containing some gas. The first pipe contains water, and it shows a level difference  $h_1=10\text{cm}$ . What is the density of the liquid in the other pipe, if the level difference in that pipe is  $h_2=15\text{cm}$ ? The open ends of both pipes are exposed to the atmosphere.

