MATH 7: HANDOUT 22 REVIEW PROBLEMS

- 1. Find the coordinates of the points where the circle $(x + 2)^2 + (y 4)^2 = 5$ meets the line y = -2x + 4.
- **2.** Write equation of a line passing through point (4, 4) and parallel to line y = 7/2x 4.
- **3.** Draw graph of function y = |x 1|. Then reflect this graph over *x*-axis and *y*-axis and plot the corresponding function. What is the equation of this graph?
- **4.** Expand as sum of powers of x: $(2x + 5)^4$
- **5.** Plot the following parabolas and determine the region where they are less than zero [Hint: use completion of the square method and find the roots].

(a)
$$y = x^2 + 2x + 3$$

(b)
$$y = -x^2 + 6x - 9$$

6. Factor the following expressions:

(a)
$$p^4 - 4z^{12}$$

(b)
$$t^2 - 3/2t + 1/2$$

- 7. Solve inequality: |x 2| > 3
- 8. An arithmetic sequence has first term $a_1 = a$ and common difference d = -1. The sum of the first *n* terms is equal to the sum of the first 3n terms. Express *a* in terms of *n*.
- **9.** Calculate the sum:

$$\frac{1}{3} + \frac{1}{3^2} + \frac{1}{3^3} + \dots + \frac{1}{3^{10}}.$$

What is the sum of the following infinite sum?

$$\frac{1}{3} + \frac{1}{3^2} + \frac{1}{3^3} + \dots$$

10. Solve the following inequalities:

(a)
$$(x+3)(x-2)^2 \le 0$$

(b) $\frac{x-2}{x+3} \le 3$

11. If we toss a coin 10 times, what is the probability that all will be heads? that there will be exactly one tail? exactly 2 tails?