Math 7a: Math Battle

December 19, 2021

- 1. There are 10 students in a class, and they are given an exam with 10 problems in it. Each student solves a different number of problems and a total of 50 problems are solved by all students together. John solved problems 1-5. Did he also solve some other problem?
- 2. A 179 \times 57 rectangle is divided into 1 x 1 squares. If we draw a diagonal in this rectangle, how many squares will it intersect?
- 3. One line divides a plane into 2 areas. Two lines can divide plane into 4 areas. What is the minimal number of lines to divide a plane into 50 areas?
- 4. If numbers 10 15 are placed on the sides of the triangle so that each side adds up to the same number, what is the largest sum each side can have?



5. In a square with the side 3, CM and CN divide its area into 3 equal parts. What is the length of CM?



6. A sum of digits in some number is equal to 4701. Is this number a full square of a natural number?