## MATH 5 — PREREQUISITES FOR MATH 6

## 1. Program

- Algebraic expressions. Commutativity, associativity, distributivity.
- Equations. Solving word problems with equations.
- Powers of 2.
- Binary numbers.
- Powers. Negative powers. Scientific notation.
- $a^2 b^2 = (a b)(a + b)$
- Square roots.
- Pythagorean theorem.
- Basic probability theory: addition rule, complement rule, product rule.
- Geometry: parallel lines and angles (alternate interior, alternate exterior, corresponding).
- Parallelogram, various definitions, properties.
- Congruence tests for triangles (SAS, ASA, SSS).
- Isosceles triangle. Median, bisector, height.
- Trapezoid. Its midline. Area.

## 2. Problems

1. Rewrite each of the expressions below in the simplest possible form, by collecting the like terms if possible.

 $2x + 7 + 5x + 2 + 3x \qquad 3x + 9 + 5xy + 2xy + 3 \qquad 3(2x - 1) + x$  $2a(a - 2) - a(a - 1) \qquad (2x - 1)(x + 1)$ 

- 2. An apple cost 9 cents, and an orange 15 cents. Elena bought some apples and oranges, 20 fruit in all, and paid \$2.64. How many apples and how many oranges did she buy?
- **3.** A boy had a bag of apples. He gave 1/2 of them to his parents, 1/5 to his brother, 1/4 to his sister and the last apple he ate himself. How many apples did he originally have?
- 4. If you take half my age and add 7, you get my age 13 years ago. How old am I?
- **5.** Simplify the following expressions

(a) x + 4(1 - x) (b) 2 + 5x - 4(3 - x) (c) 5(x - 1) - 3(2x + 1)

- 6. If you take half my age and add 7, you get my age 13 years ago. How old am I?
- 7. Two secretaries, Barbara and Mary, need to type a 100 page document. Barbara can type it in 4 hours; Mary types slower, so it would take her 5 hours to do this. How fast can they type it together if they divide the work between two of them in the most efficient way?
- 8. Find the sum  $1 + 2 + 4 + \cdots + 2^n$  (the answer, of course, will depend on n). [Hint: first try computing it for several small values of n: find 1 + 2, then 1 + 2 + 4, then 1 + 2 + 4 + 8. See if you can notice a pattern. After this, try formulating a general rule.]
- 9. Convert the decimal numbers to binary: 9, 12, 24, 38, 45
- 10. Convert the following binary numbers to decimal: 101, 1001, 10110, 11011, 10101
- 11. Compute  $110101_b + 111011_b$  without converting numbers to decimal form.