

CS 201 Homework 3/13/2022

Submit your code in Google classroom.

This problem is adopted from CMIMC 2021, Optimization round.

Start with $X = \text{list}(\text{range}(1, 401))$.

Using the elements of X (that is, integers from 1 to 400), create two new lists, A and B , such that when you multiply elements of A by elements of B , all possible products are UNIQUE. That is, you cannot have duplicate products.

ALSO: A and B must be of equal size.

Your goal is to construct the largest possible A and B lists (that is, as many elements as possible). Write a Python script to construct A and B .

Some examples:

$A = [1, 2, 3]$, $B = [1, 5, 6, 7]$ – this is not a correct entry because A has 3 elements and B has 4 elements.

$A = [1, 2, 11]$, $B = [4, 8, 11]$ – this is not a correct entry because $1 * 8 = 8$ and $2 * 4 = 8$. Thus, there are products that are not unique.

$A = [1, 2, 3, 4]$, $B = [1, 5, 6, 7]$ – CORRECT entry. You can verify that all products are unique. And both A and B are of equal size. Since $\text{len}(A) = 4$, you get 4 points.

(Notice that $1 * 6 = 6$ and $2 * 3 = 6$. However, this is NOT a problem since $2 * 3 = 6$ is the product when both numbers are the elements of A . We only require unique products when elements of A and multiplied by elements of B).