

- **1 Mole [mol]** of any substance contains the same number of molecules, called **Avogadro Number**:

$$N_A \approx 6.02 \cdot 10^{23} \frac{1}{mol}$$

- **Molar Mass,  $\mu$  [g/mol]** is the mass of 1 mole of a given substance. To find it, you need to add up **atomic weights** of all the atoms in a single molecule. Those can be found in Periodic Table.

**Example:**

$$\mu_{H_2O} = (2 + 16) \frac{g}{mol} = 18 \frac{g}{mol}$$

	Volume	Mass	Amount of Substance	Number of Molecules
<b>Symbol</b>	<b>V</b>	<b>M</b>	<b>n</b>	<b>N</b>
<b>Units</b>	[m <sup>3</sup> ] or [cm <sup>3</sup> ]	[kg] or [g]	[mol]	<b>1</b>



$$\rho = \frac{M}{V}$$

Greek 'rho'

$$n = \frac{M}{\mu}$$

Greek 'mu'

$$V = \frac{N}{N_A}$$

# Ideal Gas Law (revisited)

Classical version (with moles)

$$PV = nRT$$

Here  $n = \frac{m}{\mu}$  is amount of substance (in moles),  
 $R \approx 8.3 \frac{J}{mol \cdot K}$  is called Universal Gas Constant.

“Molecular” version

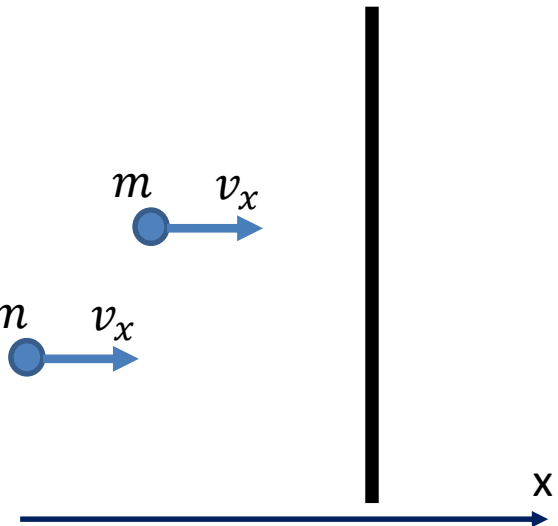
$$PV = Nk_bT$$

Here  $N = n \cdot N_A$  is number of molecules,  
 $k_B = \frac{R}{N_A} \approx 1.36 \cdot 10^{-23} \frac{J}{K}$   
is called Boltzmann Constant

Kinetic energy per degree of freedom is

$$\frac{mv_x^2}{2} = \frac{k_bT}{2}$$

$$PV = Nm v_x^2$$

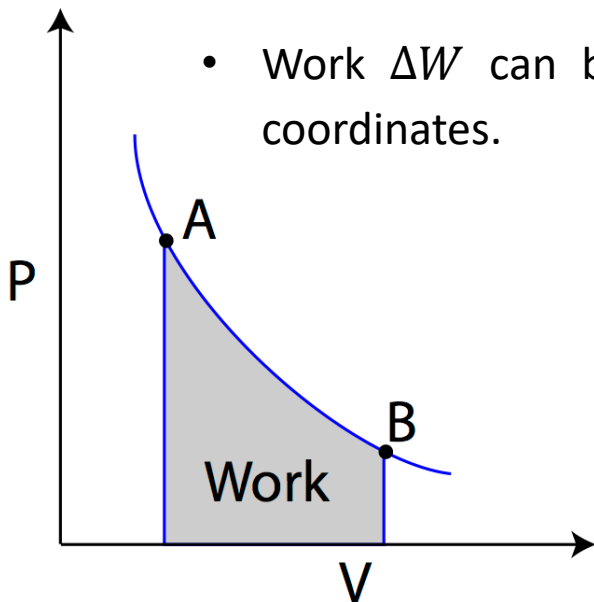


Results of Boltzmann's kinetic theory: pressure of molecules bombarding the wall.

# Applying the 1<sup>st</sup> Law of Thermodynamics to ideal gas

$$\Delta Q = \Delta E + \Delta W$$

- $\Delta Q$  - total heat adsorbed by gas
- $\Delta E$  – change in internal energy,  $\Delta E = nC_V\Delta T$ . Here  $C_V$  is specific heat per mole at constant volume, can be found as  $C_V = dR/2$  (d-number of degrees of freedom per molecule, R is universal gas constant)
- Work  $\Delta W$  can be found as an integral  $\int PdV$ , or area under P(V) plot coordinates.



## Problem 1

What is the number of molecules in a room of size  $4 \times 5 \times 2.5$  meters, at normal conditions ( $T=300K$ ,  $P= 100kPa$ )? Find the total kinetic energy of these molecules, associated with translational motion and rotation (most of those molecules are nitrogen and oxygen).

## Problem 2

Below is PV diagram for 1 mole of gas. Find the change in internal energy, work done by the gas, and the total heat adsorbed by it during this process. Initial and final states are:  $(0.02 \text{ m}^3, 100 \text{ kPa})$  and  $(0.03 \text{ m}^3, 150 \text{ kPa})$ . Specific heat of gas at constant volume is  $C_V = 20 \text{ J/K/mol}$ . Note that  $PV=RT$  for for  $n=1$  mole.

