## MATH 7: HANDOUT 20 COORDINATE GEOMETRY 4: PARABOLAS. ADDITION OF GRAPHS

## PROPERTIES OF A PARABOLA

A parabola is the set of all points in a plane that are equally distant away from a given point and a given line (see black dotted lines).

This given point is called the **focus** (black dot) of the parabola and the line is called the **directrix** (green line). If the parabola is of the form  $(x-h)^2 = 4p(y-k)$ , the vertex is (h,k), the focus is (h,k+p) and directrix is y = k-p



ADDING GRAPHS

Now that we know how to draw a lot of basic graphs and how to use transformations, we can draw more complicated graphs — that is, graphs that are we get by adding two functions.

For example, if we want to draw a graph of a function

$$y = x^2 + \frac{1}{x}$$

we can carefully examine graphs of  $y = x^2$  (blue) and y = 1/x (green), and then see what happens if one adds these two graphs (red).



## Homework

- **1.** Graph  $x^2 = 4y$ . What is the focus, directrix and vertex of the parabola?
- **2.** Sketch the following functions:
  - (a) y = |x| + |x + 1|(b) y = |x - 1| + |x + 1|(c) y = |x - 1| - |x + 1|
  - (d) |y| = x

[Hint for this problem and the next one: Draw the graphs of each of the summands separately, and then try to add the graphs.]

**3.** Sketch the following functions:

(a) 
$$y = x + \frac{1}{|x|}$$
  
(b)  $y = \sqrt{x} + \frac{1}{x}$   
(c)  $y = x - \frac{1}{x^2}$ 

- \*4. Find all intersection points of parabola  $y = x^2$  and the circle with radius  $\sqrt{6}$  and center at (0, 4).
- \*5. Let *A* and *B* be points with coordinates (a, r) and (b, s). Then let *N* be the point with coordinates (b-a, s-r), and let *O* be the origin (0, 0). Prove that  $ON \cong AB$ . (Hint: prove that ABNO is a parallelogram by proving that its diagonals bisect each other.)