

Homework problems

Instructions: Please always write solutions on a *separate sheet of paper*. Solutions should include explanations. I want to see more than just an answer: I also want to see how you arrived at this answer, and some justification why this is indeed the answer. So **please include sufficient explanations**, which should be clearly written so that I can read them and follow your arguments.

ALL GRAPHS/POINTS/FIGURES SHOULD BE DRAWN BY YOU - NOT PRINTED! USE QUADRILE PAPER!

- For what values of a does the polynomial $x^2 + ax + 14$ have no roots? exactly one root? two roots?
- Let x_1, x_2 be the roots of the equation $x^2 + 3x + 4 = 0$. Without calculating the roots, find:
 - $x_1^2 + x_2^2$ Hint: use the Vieta's formulas
 - $\frac{1}{x_1^2} + \frac{1}{x_2^2}$
- A circle with center $(3, 5)$ intersects the y -axis at $(0, 1)$.
 - Find the radius of the circle
 - Find the coordinates of the other point of intersection on the y -axis
- Convert to vertex form (use completing the square method or find the coordinates of the vertex method) and draw the following graphs:
 - $y = x^2 - 5x + 5$
 - $y = x^2 - 4x + 2$
 - $y = x^2 - x - 1$
- Convert to vertex form and draw the following graphs. On the graph show the vertex point, the focus point, and the directrix line. You will have to calculate their coordinates/equations first.
 - $y = -x^2 + 3x - 0.5$
 - $y = x^2 + 4x - 4$
- Graph $y = (\sqrt{x})^2$. Note that the domain of the function is $x \geq 0$.
- A triangle ABC has corners $A(-3, 0)$, $B(0, 3)$ and $(3, 0)$. The line $y = \frac{1}{3}x + 1$ separates the triangle in 2. What is the area of the piece lying below the line?