

MATH 6: HANDOUT 14

1. ALGEBRA: FORMULAS FOR FAST MULTIPLICATION AND FACTORIZATION

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$(a - b)^2 = a^2 - 2ab + b^2$$

$$(a + b)(a - b) = a^2 - b^2$$

$$ab + ac = a(b + c)$$

2. HOMEWORK

1. Factor:

- a. $6a + 12 =$
- b. $mn + n =$
- c. $5xy - 15x =$
- d. $4ax - 8ax^2 + 12ax^3 =$

2. Factor using formulas for fast multiplication:

- a. $9 - x^2 =$
- b. $x^6 - 4 =$
- c. $9 - 6x + x^2 =$
- d. $a^3 - 2a^2x + ax^2 =$

3. Show that the left hand side (LHS) = right hand side (RHS):

- a. $(m - n)(a + b) + m - n = a(m - n) + (b + 1)(m - n)$
- b. $x^2(x + 1) - x - 1 = x(x + 1)^2 - (x + 1)^2$
- c. $2x(x + b) + a(x + b) = (2x + a)x + (2x + a)b$
- d. $(a + b)^2 + c(a + b) = (a + b)(a + c) + (a + b)b$

4. Solve the equations:

- a. $2x(x - 1) = 2(x^2 - 5)$
- b. $\frac{1}{6}x - \frac{2}{9}(x + 5) = -\frac{1}{19}(x - 1)$
- c. $3x^2 - (3x + 2)(x - 1) - (x + 2) = 0$

5. Solve the equations:

- a. $|7x + 3| = 18$
- b. $|x + 17| = -3$
- c. $-|x + 2| + 3 = 0$

6. You are in a chemistry class and you are given a 5l solution which contains 8% sugar. How many l of 15% sugar solution do you have to add to obtain a:

- a. 10% solution
- b. 16% solution