

MATH5 CLASSWORK 20

March 21, 2021

Recall: Square root of a (denoted \sqrt{a} is a number whose square is equal to a . For example: square root of 25 is 5, because $5^2 = 25$.

We discussed that

$$\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$$

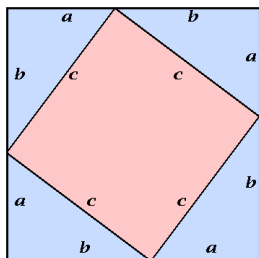
$$\sqrt{a + b} \neq \sqrt{a} + \sqrt{b}$$

Square roots naturally appear in geometry:

Pythagorean Theorem: In a right triangle with legs a , b and hypotenuse c , one has

$$a^2 + b^2 = c^2 \quad \text{or} \quad c = \sqrt{a^2 + b^2}$$

A proof of this theorem is illustrated below:

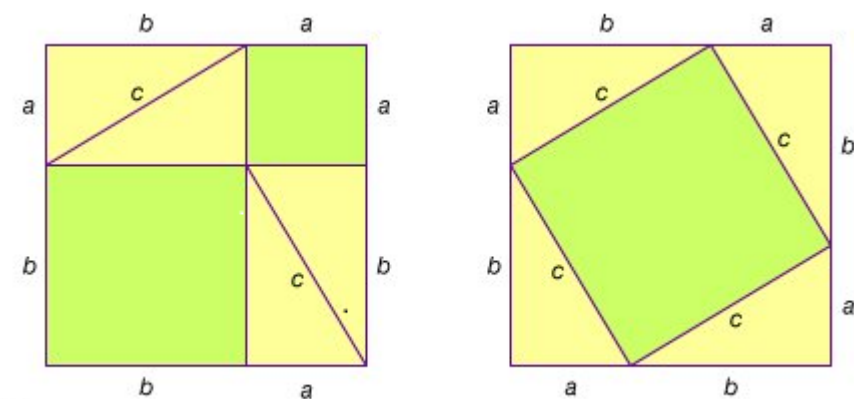
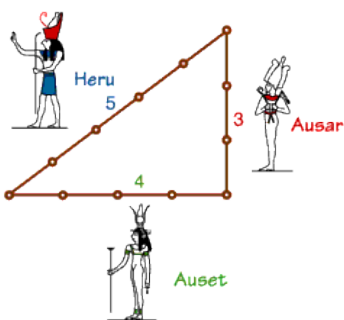


In this square, the total area is

$$(a + b) \times (a + b) = a \times (a + b) + b \times (a + b) = a^2 + ab + ab + b^2 = a^2 + 2ab + b^2$$

On the other hand, the area of each triangle is $\frac{1}{2}ab$; and the area of shaded square is c^2 . Thus, we get $a^2 + 2ab + b^2 = 4 \cdot \frac{1}{2}ab + c^2$, which gives


$$a^2 + b^2 = c^2$$






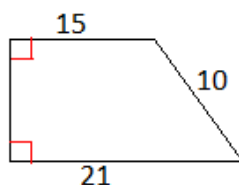
© 2002 Encyclopædia Britannica, Inc.

MATH5 HOMEWORK 20

March 21, 2021

Please make sure your solutions for the problems with  are accompanied by a picture done with a ruler and a pencil. Drawing a problem will help you to solve it.

-  Can you find a right triangle where all sides are whole numbers and the hypotenuse is 13?
-  If, in a right triangle, one leg has length 1 and the hypotenuse has length 2, what is the other leg?
- Find $\sqrt{2^6 \cdot 7^2}$ [use square root properties we discussed]; $\sqrt{\frac{1}{16}}$; $\sqrt{\frac{4}{9}}$.
-  Find the height and area of the figure below. Lengths of three sides are given; the two marked angles are right angles.



- Take some positive number $x < 100$ and using calculator (or computer) calculate the number $\frac{x}{2} + \frac{1}{x}$. Call the result x and repeat the same calculation with the new x . Do it 10 times. We will compare the results in class.

x	$\frac{x}{2} + \frac{1}{x}$
Initial x	result_1
result_1	result_2
result_2	result_3
result_3
.....
result_9	result_10

- What the artist wanted to tell? Use mathematical language to explain, name what you need.

