

Classwork 19. Algebra.

Algebra.

Inequalities.

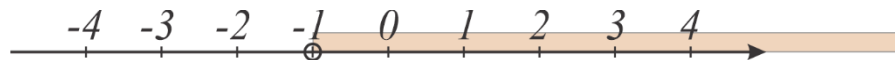
There is another type of problems, when we need to find all possible values of variable which are greater (or smaller) than a particular number. In more sophisticated case, for which values of variable, one expression is greater (smaller) than another expression, for example:

$$x + 3 > 2x - 5$$

The simplest inequality is

$$x > a, \quad x < a, \quad \text{where } x \text{ is variable and } a \text{ is a number.}$$

$x > -1$, the solution is all x , greater than 1,



Solution can be shown graphically as $x \in (-1, +\infty)$, or can be left as it is, it's already a solution (similarly as a solution of an equation $x = 2$.)

We can add any number to both parts of the inequality, the sign ($<$ or $>$) will not change:

$$x > -1$$

$$x + 2 > -1 + 2 \Rightarrow x + 2 > 1$$

$$y - 3 < 5$$

$$y - 3 + 3 < 5 + 3$$

$$y < 8, \quad y \in (-\infty, 8)$$

$$1. \quad x + 3 > -5$$



Now let's try to multiply or divide both parts of the inequality by the positive number.

If $x > 3$, then $2x$ will be greater than 6.

$$x > 3, \quad 2x > 6$$

If $x > 3$ what can we tell about $-x$?

$$-x \quad 3 \cdot (-1)$$

2. $x + 3 > 5x - 5$

3. $4x - 3 \neq 0$

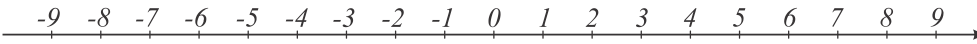
4. $3(x - 1) < 5x + 9$

5. $2x - 1 > -x + 3$

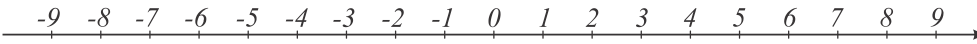
6. $|x| > 8$

7. Show on the number line points that are satisfying the following inequalities:

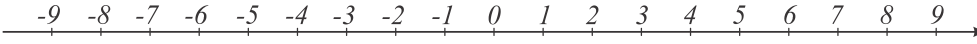
a) $|x| < 4$



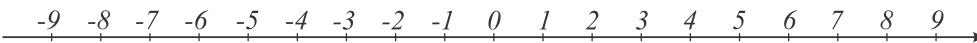
b) $|x| > 3$



c) $\left|x - \frac{1}{2}\right| > 3$



d) $\left|x - \frac{1}{2}\right| < 8$



8. $M = \{x | x > 5\}$, $K = \{x | x < 20\}$

$$M \cap K =$$

$$M \cup K =$$

9. $M = \{x | x \leq 5\}$, $K = \{x | x \geq 20\}$

$$M \cap K =$$

$$M \cup K =$$

10. Points a , 0 , and b are marked on the number line below:



Which of the following expressions is true?

- 1) $a + b > 0$ or $a + b < 0$ 3) $ab > 0$ or $ab < 0$
 2) $a - b > 0$ or $a - b < 0$ 4) $\frac{b}{a} > 1$ or $\frac{b}{a} < 1$

11. Points $a, b, c, 0$, and 1 are marked on the number line below:

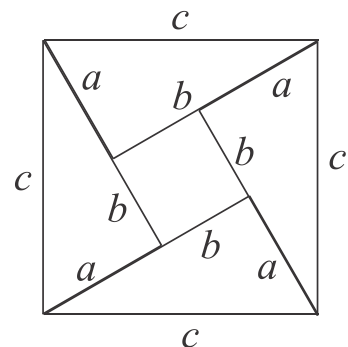
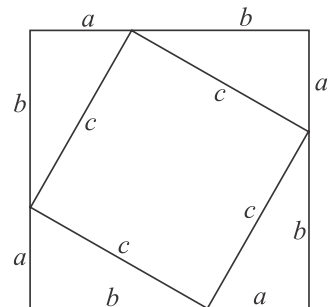


Which of the following expressions is true?

- 1) $ab < b$ or $ab > b$
 2) $abc < a$ or $abc > a$
 3) $-ac < c$ or $-ac > c$

Pythagorean theorem.

4 identical right triangles are arranged as shown on the picture. The area of the big square is $S = (a + b) \cdot (a + b) = (a + b)^2$, the area of the small square is $s = c^2$. The area of 4 triangles is $4 \cdot \frac{1}{2}ab = 2ab$. But also can be represented as $S - s = 2ab$
 $2ab = (a + b) \cdot (a + b) - c^2 = a^2 + 2ab + b^2 - c^2$
 $\Rightarrow a^2 + b^2 = c^2$



12. The legs of a right triangle are 3, 4 cm. What is the hypotenuse?
 13. The legs of a right triangle are 5 and 8 cm. What is the hypotenuse?
 14. Hypotenuse of a right triangle is 12 cm and the leg is 10 cm. Find another leg.