## Black body radiation

We have discussed the radiation spectrum of a black body. We learned that spectral radiant exitance of a black body can be expressed as:

$$R(\lambda, T) = \frac{2\pi hc^2}{\lambda^5} \cdot \frac{1}{e^{\frac{hc}{\lambda kT}} - 1}$$
 (1)

It looks a bit too complicated, but just for a first glance. Here h is the Planck's constant,  $\underline{\mathbf{c}}$  is the speed of light,  $\lambda$  is the wavelength, T is the temperature in absolute units (Kelvin scale), k is the Boltzmann constant ( $k = 1.38 \cdot 10^{-23} J/K$ ) and e is mathematical constant, often referred as the Euler's number or Napier's number ( $e \approx 2,718281828$  ....). As the famous P number, e is irrational so there is no period in the mantissa of e.

What does the expression (1) mean? It shows the energy per unit wavelength, emitted from unit area of a black body at temperature T in a narrow wavelength range near the wavelength  $\lambda$ . It shows the contribution of different wavelengths to the total power, emitted by a black body. The plots of the spectral radiant exitance of a black body at different temperatures are shown in Figure 1.

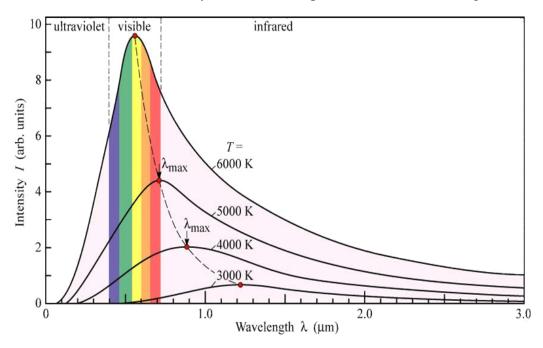


Figure 1. Schematic plots of the expression (1) at different temperatures. (the image is taken from <a href="http://www.globalchange.umich.edu/globalchange1/current/lectures/universe/universe.html">http://www.globalchange.umich.edu/globalchange1/current/lectures/universe/universe.html</a>)

## Problems:

- 1. Find units of  $R(\lambda, T)$  and explain the result.
- 2. Please simplify the expression (1) for the case of  $\frac{hc}{\lambda kT} \ll 1$ . For this one can use a following mathematical approximation: if  $x \to 0$ , then  $e^x \approx 1 + x$ .