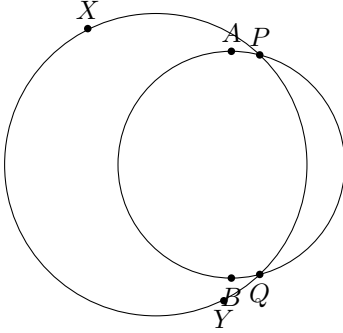
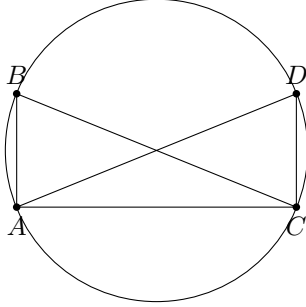


1. HOMEWORK

- Let A, B, C, D be points on circle ω that form a quadrilateral. Prove that $m\angle ABC + m\angle ADC$. We call such a quadrilateral a **cyclic quadrilateral**: it is inscribed in a circle.
- Let A, B, C be on a circle centered at O such that $\angle AOB \cong \angle BOC \cong \angle COA$. Prove that $\triangle ABC$ is an equilateral triangle.
- Given points A, B , what is the locus of points C such that $m\angle ACB = x^\circ$ for some number x ? (Assume $0 < x < 180$)
- Let λ be a circle whose center is inside circle ω such that λ, ω intersect at points P, Q . Let \overline{AB} be a diameter of λ such that A, B are on λ and inside ω ; then, let \overleftrightarrow{PA} and \overleftrightarrow{PB} intersect ω at points X, Y respectively. Prove that \overline{XY} is a diameter of ω .



- Let $\triangle ABC$ and $\triangle ADC$ be right triangles such that A, B, C, D lie on a circle and $m\angle BAC = 90^\circ$. Prove that $ABCD$ is a rectangle.



- Given a line segment \overline{AB} such that $AB = 1$, construct C on \overline{AB} such that:
 - $AC = \frac{1}{4}$
 - $AC = \frac{1}{3}$
 - $AC = \frac{1}{6}$
 - $AC = \frac{1}{5}$
 - $AC = \sqrt{2}$
 - $AC = \sqrt{3}$
 - $AC = \sqrt{5}$
 - $AC = \sqrt{7}$

- Let $ABCD$ and $ABEF$ be parallelograms such that E, F are on the line \overleftrightarrow{CD} ; let the diagonals \overline{AC} , \overline{BD} intersect at M and \overline{AE} , \overline{BF} intersect at N . Prove that $\overline{MN} \parallel \overline{AB}$.

