MATH 6 HOMEWORK2: SOLVING EQUATIONS AND INEQUALITIES

SOLVING INEQUALITIES INVOLVING NEGATIVE NUMBERS

Today we discussed inequalities and their solutions, discussing how one solves inequalities involving negative numbers. The rule here is

$$a < b \iff (-a) > (-b)$$

(note that the sign of inequality is reversed!). For example, 3 < 5, but -3 > -5.

More generally, if we multiply or divide both sides of an inequality by a negative number, we need to change the sign of inequality, replacing $\langle by \rangle$ and vice versa. For example, to solve -3x > -6, we divide both sides by -3 and change \rangle to $\langle giving x \langle 2 \rangle$.

Products

The following rules are frequently used when dealing with equations or inequalities where the left-hand side is a product of two factors:

• A product of two numbers is zero if and only if one of them is zero:

$$ab = 0 \iff (a = 0) \text{ or } (b = 0)$$

• A product of two numbers is positive if and only if both numbers are positive or both numbers are negative:

 $ab > 0 \iff (a > 0 \text{ and } b > 0) \text{ or } (a < 0 \text{ and } b < 0)$

• A product of two numbers is negative if and only if one of numbers is positive and the other one is negative:

 $ab < 0 \iff (a > 0 \text{ and } b < 0) \text{ or } (a < 0 \text{ and } b > 0)$

Homework

1. (This problem is for students who have some difficulty with negative numbers and need extra practice).

Compute the following expressions:

$$\begin{array}{rl} -3 - (-2) & -3 - 3 & ((-4) \times 6) - 7 \\ (-6) \div (-2) + 3 & (-2) \div (-3) & (-4) \times (-7) \div (+9) \\ (-4) - (-3) + (-5) & (-6) + (-2) \div (-3) \end{array}$$

2. Solve the following inequalities

(a)
$$-x < 2$$
 (b) $2 - 3x > 5$ (c) $3x + 1 < 5x + 7$
(d) $1 + 5x < 3x$ (e) $x - 1 < x - 7$

3. Solve the following equations and inequalities:

(a) (x-1)(x-2) = 0 (b) x(x+1) < 0 (c) $\frac{1}{x} > 2$ [Hint: multiply by x] (d) $x^2 - 4 = 0$ (e) $\frac{x}{x+1} > 1$ [Hint: consider separately two cases: x + 1 > 0 and x + 1 < 0] 4. In the figure below, each symbol stands for a number. The sum of numbers in each column or row is written next to the column or row — except for the second column, where the sum is not known. Can you find this missing sum?



- 5. Old MacDonald raises sheep and chickens on his farm. His livestock has a total of 55 heads and 142 legs among them (not counting the farmer!). How many chickens and how many sheep does he have?
- 6. Mr. Sim jogs at 9 km per hour over a certain distance and walks back the same distance at 6 km per hour. What is his average speed? [Hint: the answer (6+9)/2 = 7.5 is wrong!).
- 7. Show that in a class of 40 students, there must be two students whose birthdays are less than 10 days apart. '
- 8. January 1, 2018 was a Monday. What is the next year in which January 1 will fall on a Monday? (Mathcounts)
- 9. Find AB (Mathcounts).



10. Three cubes are stacked as shown. If the cubes have edge 1,2 and 3 what is AB? (Mathcounts)

