

TODAY'S MEETING

Today we continued to talk about collision problems. We solved homework problems from the last meeting.

We started to talk about oscillations using $F = ma$ exam problems as examples. Generally one can find the frequency, and period of small oscillations using either equations of motion

$$(1) \quad \ddot{x} = -\omega^2 x,$$

or energy conservation equation

$$(2) \quad E = \frac{M}{2} (\dot{x}^2 + \omega^2 x^2).$$

If one can bring equations of motion for a given system to either form (1) or (2), one can immediately find the angular frequency ω or period $T = 2\pi/\omega$ or frequency $f = 1/T$ of oscillations.

For example, for the harmonic oscillator mass+spring we have

$$\begin{aligned} \ddot{x} &= -\frac{k}{m}x, \\ E &= \frac{m}{2} \left(\dot{x}^2 + \frac{k}{m}x^2 \right), \\ \omega &= \sqrt{\frac{k}{m}}, \quad T = \frac{1}{f} = 2\pi\sqrt{\frac{m}{k}}. \end{aligned}$$

For pendulum

$$\begin{aligned} \ddot{\phi} &= -\frac{g}{L} \sin \phi \approx -\frac{g}{L} \phi, \\ E &= \frac{mL^2}{2} \left(\dot{\phi}^2 + \frac{2g}{L}(1 - \cos \phi) \right) \approx \frac{mL^2}{2} \left(\dot{\phi}^2 + \frac{g}{L}\phi^2 \right), \\ \omega &= \sqrt{\frac{g}{L}}, \quad T = \frac{1}{f} = 2\pi\sqrt{\frac{L}{g}}. \end{aligned}$$

We solved the problems 12,13,19,23,25 of $F = ma$ 2015

<https://aapt.org/physicsteam/2015/upload/exam1-2015-1-8.pdf>

HOMEWORK PROBLEMS

1. Solve problems 7, 14, 15 of $F = ma$ 2016

<https://www.aapt.org/physicsteam/2016/upload/exam1-2016-3-1-2.pdf>

2. Solve problems 11, 12, 14, 24 of $F = ma$ 2018A

<https://www.aapt.org/physicsteam/2019/upload/Fma-2018-A.pdf>

IMPORTANT

The next club meeting is on January 26, 2020. We will start discussing PhysicsBowl exam. Good luck to everybody taking $F=ma$ exam this week!