Math 9 placement test

1. Open brackets and expand the following expressions

a.
$$(a+b)^2 =$$

b.
$$(a - b)^3 =$$

2. Factor the following expressions

a.
$$a^2 - b^2 =$$

b.
$$a^3 - b^3 =$$

c.
$$a^3 + b^3 =$$

d.
$$1 + a + a^2 + a^3 =$$

- 3. Find the coefficient of x^5 in the expression $(1 + 2x)^8$
- 4. Find the remainder of 3^{2014} upon division by 7.
- 5. Solve the equation

$$\frac{x^2+1}{2x} + \frac{2x}{x^2+1} = 2$$

- 6. Eight teams have reached the quarter-finals of the soccer World Cup.
 - a. How many ways are there for these teams to be paired to play the quarter-final games?
 - b. How many different outcomes of which team wins which medal (gold, silver, bronze) are possible?
- 7. Corners of a square with the side a are cut off so that a regular octagon is obtained. Find the area of this octagon.