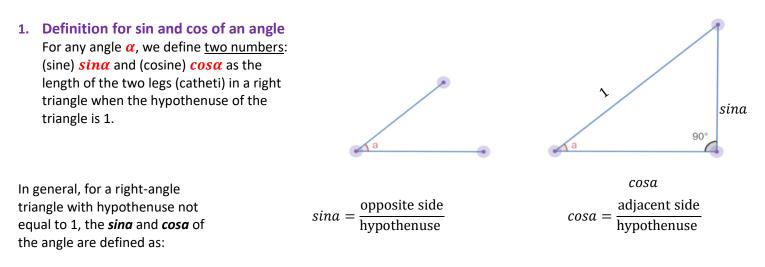
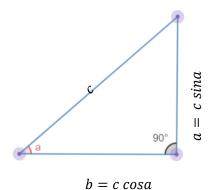
## Math 7 Homework 16: Trigonometry, basic definitions.



This is because the definitions on *sin* and *cos* do not really depend on size of the triangle, but only the angle itself. Since any two right triangles with the same angles are similar, it shows that if we have a right triangle with angle  $\alpha$  and hypotenuse **c**, then the sides will be *c sin*  $\alpha$  and *c cos*  $\alpha$ :

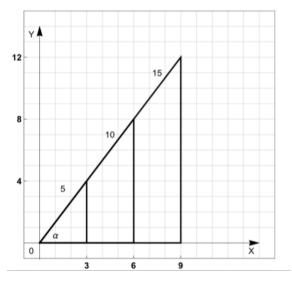


sina =	opposite side	-csina	
sinu –	hypothenuse	C	
	adjacent side	_ c cosa	
cosa =	hypothenuse	$=\frac{1}{c}$	

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**Example**: Consider the angle a in the following triangles:



$$sina = \frac{\text{opposite side}}{\text{hypothenuse}} = \frac{4}{5} = \frac{8}{10} = \frac{12}{15}$$
$$cosa = \frac{\text{adjacent side}}{\text{hypothenuse}} = \frac{3}{5} = \frac{6}{10} = \frac{9}{15}$$

2. Table with values for trigonometric functions

Function	Notation	Definition	<b>0</b> <sup>0</sup>	<b>30</b> <sup>0</sup>	45 <sup>0</sup>	<b>60</b> <sup>0</sup>	<b>90</b> <sup>0</sup>
sine	sin(a)	opposite side hypothenuse	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1
cosine	cos(a)	adjacent side hypothenuse	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0

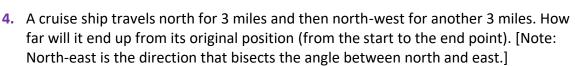
## Homework problems

*Instructions:* Please always write solutions on a *separate sheet of paper*. Solutions should include explanations. I want to see more than just an answer: I also want to see how you arrived at this answer, and some justification why this is indeed the answer. So **please include sufficient explanations**, which should be clearly written so that I can read them and follow your arguments.

## All angles are measured in degrees.

- 1. Which one is greater?
  - a. 0 or sin  $0^0$ 
    - b.  $1 \text{ or } \sin 30^{\circ}$

- c.  $\sin 45^{\circ} \text{ or } \cos 45^{\circ}$
- d.  $\cos 60^\circ \text{ or } \sin 30^\circ$
- 2. A tree casts a 60 m long shadow when the angle of elevation of the sun is 30<sup>0</sup>. How tall is the tree? [Angle of elevation is the angle that line from tip of shadow on ground to top of tree makes with the horizontal.]
- A ladder of length L is resting on a ledge whose height is half of the ladder's length. The ladder makes a 45<sup>o</sup> angle with the ground. Express answers in terms of L.
  - a. How long is the portion of the ladder between the ground and the point of contact of ledge and ladder? [indicated by a long dashed arrow]
  - b. At what height is the top of ladder above the ledge? [indicated by short dashed arrow - this is another right triangle.]



5. A ship travels for 3 miles north, then turns and goes for 2 miles northeast, then for another 5 miles north-northeast. Where will it be at the end - how far east and north of the original position? [Northeast means that its direction bisects the angle between north and east directions, thus forming an angle of 45° with due north. North-northeast means that this direction bisects the angle between north and 22.5° angle with due north.]

6. Consider a regular pentagon inscribed in a circle of radius 1. What is the side length of such a pentagon? [Hint: drop a perpendicular from the center to one of the sides and complete it to form a right triangle.]

- 7. (\*) Consider a parallelogram ABCD with AB = 1, AD = 3,  $\angle A = 40^{\circ}$ . Find the lengths of diagonals in this parallelogram.
- 8. Prove that the area of a triangle ABC can be computed using the formula  $A = \frac{1}{2} \cdot AB \cdot AC \cdot sin \angle A$ . [Hint: what is the altitude from vertex B?]
- **9.** What is the area of a regular pentagon inscribed in a circle of radius 10? [Make sure to use a trigonometric function.]

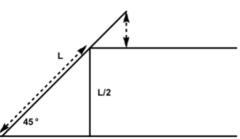


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