<u>Class Test</u> Nov. 10, 2024

1. Arithmetic sequences -summary

$$a_n = a_1 + (n-1)d$$
$$a_n = \frac{a_{n-1} + a_{n+1}}{2}$$
$$d = \frac{a_s - a_t}{s-t}$$
$$S = \frac{(a_1 + a_n) \times n}{2}$$

2. Geometric sequences -summary

$$a_n = a_1 \times q^{n-1}$$
$$a_n = \sqrt{a_{n-1} \cdot a_{n+1}}$$
$$S_n = a_1 \times \frac{(1-q^n)}{1-q}$$
$$S = \frac{a_1}{1-q}$$

Problems

Instructions: Please always write solutions on a *separate sheet of paper*. Solutions should include explanations. I want to see more than just an answer: I also want to see how you arrived at this answer, and some justification why this is indeed the answer. So **please include sufficient explanations**, which should be clearly written so that I can read them and follow your arguments.

- 1. Factorize: (2.5 points each)
 - a. $(x-3)^2 (y+3)^2$ b. $m^2 - m - 12$ c. $a^4 - 144b^{10}$ d. $x^4 + 4$
- 2. Factorize: (5 points each)
 - a. $22x^2 + 47x + 21$ b. $p^4 + 4z^{4n}$
- Solve for x: (5 points each)
 a. x²+5x = 11/4

b. $4m^2 - 49p^2q^2 = 0$

10 points for the rest of the problems.

- 4. In the arithmetic progression 5, 17, 29, 41, . . . what term has a value of 497?
- 5. The 3-rd term of the arithmetic progression is equal to 1. The 10-th term of it is three times as much as the 6-th term. Find the first term and the common difference.
- 6. Write the first 5 terms of a geometric progression if $a_1 = -25$ and $q = \frac{1}{3}$
- 7. What are the first 2 terms of the geometric progression: *a*₁, *a*₂, 24, 36, 54, ...?
- 8. What is the common ratio of the geometric progression: $\frac{1}{2}$, $-\frac{1}{2}$, $\frac{1}{2}$, $-\frac{1}{2}$, ...? What is a_{10} ? What is a_{100} ?
- 9. Calculate the sum of infinite series: $\frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \cdots$
- 10. What is the sum of : $1 2 + 2^2 2^3 + 2^4 2^5 + \dots 2^{15}$?
- 11. What is the sum of: $1 + x + x^2 + x^3 + x^4 + x^5 + \dots + x^{100}$?
- 12. A geometric progression has 99 terms, the first term is 12 and the last term is 48. What is the 50-th term?