MATH 6: HANDOUT 17 **COORDINATES II**

DISTANCE BETWEEN POINTS AND CIRCLE

The distance between two points $P(x_1, y_1)$ and $Q(x_2, y_2)$ is given by the following formula:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}.$$

This formula is a straightforward consequence of the Pythagoras' Theorem.

The equation of the circle with the center $M(x_0, y_0)$ and radius r is (

$$(x - x_0)^2 + (y - y_0)^2 = r^2.$$

This equation means, that points (x, y) should be at distance r from the given point $M(x_0, y_0)$.



GRAPHS OF FUNCTIONS

In particular, if the relation is of the form y = f(x), where f is some function of x (i.e., some formula which contains x), the set of all points whose coordinates satisfy this relation is called the graph of f.

Line. The graph of the function y = mx + b is a straight line. The coefficient m is called the slope.











GRAPH OF y = |x|

The figure below shows graphs of functions y = |x|.



1. TRASNFORMATIONS

Having these basic graphs, we can produce new graphs, by doing certain transformations of the equations. Here are two of them.

Vertical translations: Adding constant *c* to the right-hand side of equation shifts the graph by *c* units up (if *c* is positive; if *c* is negative, it shifts by |c| down.)



Horizontal translations: Adding constant c to x shifts the graph by c units left if c is positive; if c is negative, it shifts by c right.



Homework

- **1.** Find the equation of the line through (1, 1) with slope 2.
- **2.** Find the equation of the line through points (1, 1) and (3, 7). [Hint: what is the slope?]
- 3. (a) Find k if (1,9) is on the graph of y 2x = k. Sketch the graph.
 (b) Find k if (1, k) is on the graph of 5x + 4y 1 = 0. Sketch the graph.
- **4.** Let l_1 be the graph of y = x+1, l_2 be the graph of y = x-1, m_1 be the graph of y = -x+1, and m_2 be the graph of y = -x-1.
 - (a) Find the intersection point of l_1 and m_1 ; Label this point P and write down its coordinates.
 - (b) Find the intersection point of l_2 and m_2 ; Label this point P and write down its coordinates.
 - (c) Find the midpoint of *AB* and write down its coordinates.
 - (d) Let *C* be the intersection point of l_1 with m_2 , and *D* be the intersection point of l_2 with m_1 . What kind of quadrilateral is *ABCD*?
 - (e) Explain why l_1 and l_2 are parallel. What is the distance between them?
- 5. Find the intersection point of a line y = x 3 and a line y = -2x + 6. Sketch the graphs of these lines.
- 6. (a) Sketch the graphs of functions y = |x + 1| and y = -x + 0.25.
 - (b) How many solutions do you think this equation has?

$$|x+1| = -x + 0.25$$

Note: you are not asked to find the solutions — just answer how many are there.

- 7. (a) Draw the graph of the equation $x^2 + y^2 1 = 0$.
 - (b) Draw the graph of the equation $x^2 + (y-1)^2 1 = 0$.
 - (c) Draw the graph of the equation xy = 0.
 - (d) Draw the graph of the equation $x^2 + y^2 = 0$.
- 8. Sketch graphs of the following functions:

(a)
$$y = |x| + 1$$
 (b) $y = |x + 1|$ (c) $y = |x - 5| + 1$