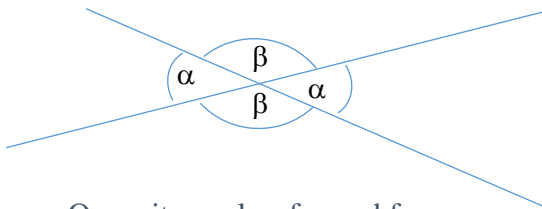


# Math 5e, Homework 22

due March 19

**Instructions:** Some of the problems we solved in class, and some are new. Please try to solve all problems, do your best, and show your work. **Write on separate sheets of paper, not between the lines of this handout!**

## Geometry: Angles , Parallel lines

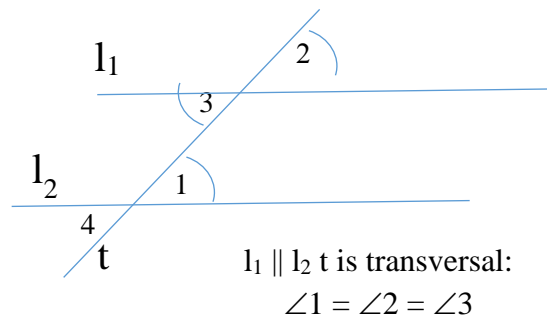


Opposite angles, formed from crossing straight lines, are equal.

$$\angle \alpha = \angle \alpha - \text{opposite}$$

$$\angle \alpha + \angle \beta = 180^\circ - \text{on a straight line,}$$

Or complementary angles

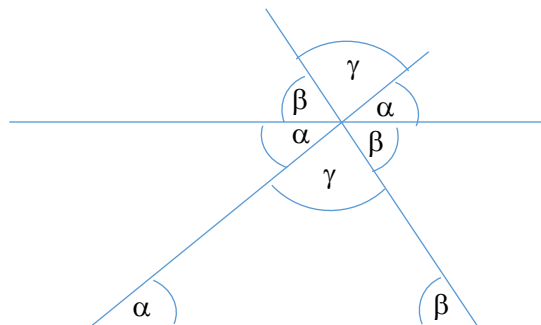


$$\angle 1 = \angle 3 = \text{alternate internal angles}$$

$$\angle 1 = \angle 2 = \text{corresponding angles}$$

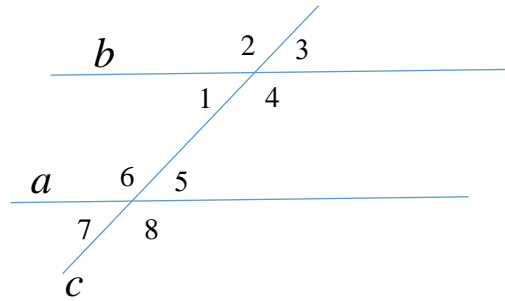
$$\angle 4 = \angle 2 = \text{alternate exterior angles}$$

From both these pieces of information we can show that the sum of angles in a triangle is always  $180^\circ$ .



## Homework

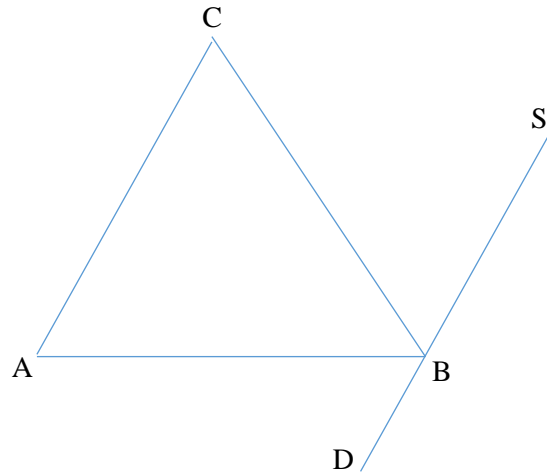
- On the picture,  $a$  and  $b$ , which are parallel to each other, are intersected by line  $c$ . What are the relationships (name the type of angles):
  - $\angle 3$  and  $\angle 5$
  - $\angle 2$  and  $\angle 8$
  - Prove (explain) that  $\angle 4 + \angle 5 = 180^\circ$ .



- In the same picture,
  - if  $\angle 7 = 65^\circ$ , find:  $\angle 1$ ,  $\angle 3$ ,  $\angle 1 + \angle 6$
  - If you know that  $\angle 7 = \angle 1$ , prove that\*:  $\angle 1 = \angle 3$  and  $\angle 5 = \angle 1$

(\* or say why the angles will be equal)

- Intersecting at point B on triangle ABC is drawn line DS, such that DS is parallel to AC. Prove that (or say why the angles will be equal):
  - $\angle ACB = \angle SBC$
  - $\angle CAB = \angle DBA$
  - $\angle CAB = \angle SBK$
  - If  $\angle CAB = 40^\circ$  and  $\angle BCA = 60^\circ$ , find angles  $\angle ABD$  and  $\angle SBC$



- In triangle ABC,  $\angle A = 35^\circ$ ,  $\angle B = 55^\circ$ , prove (explain) that this triangle is right-angled.
- What type of triangle has one angle equal to the sum of the other two?
- Find each of the outside angles of a right-triangle, if one of its angles is  $58^\circ$ .