

MATH 6 REVIEW OF MATH 5 TOPICS

1. PROGRAM

- Algebraic expressions. Commutativity, associativity, distributivity.
- Equations. Solving word problems with equations.
- Powers of 2.
- Binary numbers.
- Powers. Negative powers. Scientific notation.
- $a^2 - b^2 = (a - b)(a + b)$
- Square roots.
- Pythagorean theorem.
- Basic probability theory: addition rule, complement rule, product rule.
- Choosing with and without repetition. Permutations.
- Geometry: parallel lines and angles (alternate interior, alternate exterior, corresponding).
- Parallelogram, various definitions, properties.
- Congruence tests for triangles (SAS, ASA, SSS).
- Isosceles triangle. Median, bisector, height.
- Trapezoid. Its midline. Area.

2. PROBLEMS

1. Rewrite each of the expressions below in the simplest possible form, by collecting the like terms if possible.

$$\begin{array}{lll} 2x + 7 + 5x + 2 + 3x & 3x + 9 + 5xy + 2xy + 3 & 3(2x - 1) + x \\ 2a(a - 2) - a(a - 1) & (2x - 1)(x + 1) & \end{array}$$

2. An apple cost 9 cents, and an orange 15 cents. Elena bought some apples and oranges, 20 fruit in all, and paid \$2.64. How many apples and how many oranges did she buy?

3. A boy had a bag of apples. He gave $\frac{1}{2}$ of them to his parents, $\frac{1}{5}$ to his brother, $\frac{1}{4}$ to his sister and the last apple he ate himself. How many apples did he originally have?

4. Simplify the following expressions

(a) $x + 4(1 - x)$ (b) $2 + 5x - 4(3 - x)$ (c) $5(x - 1) - 3(2x + 1)$

5. If you take half my age and add 7, you get my age 13 years ago. How old am I?

6. Two secretaries, Barbara and Mary, need to type a 100 page document. Barbara can type it in 4 hours; Mary types slower, so it would take her 5 hours to do this. How fast can they type it together if they divide the work between two of them in the most efficient way?

7. Find the sum $1 + 2 + 4 + \cdots + 2^n$ (the answer, of course, will depend on n). [Hint: first try computing it for several small values of n : find $1 + 2$, then $1 + 2 + 4$, then $1 + 2 + 4 + 8$. See if you can notice a pattern. After this, try formulating a general rule.]

8. Convert the decimal numbers to binary:
9, 12, 24, 38, 45

9. Convert the following binary numbers to decimal:
101, 1001, 10110, 11011, 10101

10. Compute $110101_b + 111011_b$ without converting numbers to decimal form.

11. Simplify the following expression:

$$\frac{(x^2y^2) \cdot x^3}{x^2y^5}$$

12. Let $a = 2 \cdot 10^8$, $b = 10^5$. Compute $a^2 \cdot b$, $\frac{a}{b}$, $a^2 \div b^3$.

13. If $a = 2^{-13}3^9$, $b = 2^{11}3^{-7}$, what is the value of ab ? of a/b ?

14. Write the following numbers using scientific notation.

(a) the distance from Earth to Pluto is $\approx 7,527,000,000$ km;

(b) the distance from Earth to the star Sirius is $\approx 81,900,000,000,000$ km;

15. Factor the following number into primes: $99^2 - 9^2$. [Hint: you do not have to compute this number.]

16. Find the following square roots. If you can not find the number exactly, at least say between which two whole numbers the answer is, e.g., between 5 and 6.

(a) $\sqrt{81}$

(b) $\sqrt{10,000}$

(c) $\sqrt{10^8}$

17. If, in a right triangle, one leg has length 1 and the hypotenuse has length 2, what is the other leg?

18. Simplify: $(\sqrt{17})^2$, $(\sqrt{13})^4$, $(\sqrt{11})^3$, $\sqrt{2^4 3^6}$, $\sqrt{2^4 3^5}$.

19. We roll two dice. What is the probability of getting sum of two numbers equal to 4?

20. If we toss a coin 5 times, what is the probability that **at least one** will be heads?

21. A license plate consists of 3 letters, followed by three digits. How many possible license plates are there?

22. We roll two identical dice. What is the probability of getting 1 and 3?

23. We roll two identical dice. What is the probability of getting sum of two numbers equal to 4?

24. If we toss a coin 5 times, what is the probability that at least one will be heads?

25. How many ways are there to seat 15 students in a classroom which has 15 chairs?
If the room has 25 chairs?

26. Solve equations:

(a) $\frac{3}{8}x = \frac{1}{3}$

(b) $|2x - 5| = 1$

(c) $\frac{x - 2}{x - 1} = 3$