

A and G 1. Class work 27.

Algebra.

Review of sets.

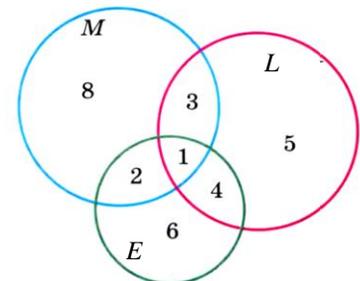


1. A set is a collection of well defined objects. We can create a set just by listing all of its elements. For example, set A contains 2,5, v, n, •, ◊. We denote, $A = \{2,5, v, n, \bullet, \diamond\}$. The second way to create a set is to describe a rule, which is applicable to all elements in the set. For example: set N is the set of natural numbers.
2. If B is a set and x is one of the objects of B, this is denoted $x \in B$, and is read as "x belongs to B", or "x is an element of B". If y is not a member of B then this is written as $y \notin B$, and is read as "y does not belong to B".
3. $C = \{2, 5\}, C \subset A$
Each element of the set C is also an element of set A, so C is subset of A.
C is also a subset of N, since 2 and 5 are natural numbers. We can write $C \subset N$.
The empty set is a subset of every set and every set is a subset of itself:

- $\emptyset \subset A$.
- $A \subset A$.

4. A set, containing elements which are common elements of two sets is called intersection of the two sets. $C = A \cap B$.
5. Two sets can be "added" together. The *union* of D and M, denoted by $D \cup M$, is the set of all things that are members of either D or M
6. We can divide set into two or more subsets in such a way that each element of the set will be in only one of these subsets, intersection of any two subsets will be an empty set. The set of non-intersecting subsets is called partition of the set. For example, the set of natural numbers N can be partitioned into two sets, of even and odd numbers. Each natural number is either even or odd.
7. $M = \{x | x > 5\}, K = \{x | x < 20\}$
 $M \cap K =$
8. $A = \{a, b, c, d\}, B = \{c, d, e, f\}, C = \{c, e, g, k\}$.
 $(A \cap B) \cap C =$
 $(A \cup B) \cup C =$

9. In the picture on the right, set M represents students of the 7-th grade, who participated in the math Olympiad, set L represents 7-th graders who participated in the Literature Olympiad, and set E represents the English Art Olympiad participants. How many students,



- a. Participated in the Math Olympiad?
- b. In the Math and English Olympiads?
- c. In the Literature and English Olympiads?
- d. In any of the three Olympiads?
- e. In all three Olympiads?
- f. In any two Olympiads?
- g. How many 7-th graders did take part in Olympiads?
- h. How many students did not participate in any Olympiad, if there are 60 students in the 7th grade?

Problems Review.

1. Two pipes fill together a pool in 1 h and 20 minutes. If the first pipe is open for 10 minutes, and the second pipe is open for 12 minutes, the pool will be filled on $\frac{2}{15}$. How fast each pipe will fill the pool?
2. Simplify the expression:

$$(x^2 + y^2 + x + y)(x + y + xy) =$$

3. In a restaurant, customer can order a cheese platter for \$15 or \$20. For \$15 platter, you can choose 3 different kind of cheese out of 15 and for \$20 platter you can choose 5 different kind of cheese. How many different ways are there to create these two cheese platters?
4. Using the algebraic identities calculate:

a. $91 \cdot 89$;

b. 61^2 ;

c. $(\sqrt{10} + \sqrt{11})(\sqrt{11} - \sqrt{10})$;

5. Simplify:

$$(\sqrt{28} - 3\sqrt{5}) - (\sqrt{7} + \sqrt{20})$$