

- **1 Mole [mol]** of any substance contains the same number of molecules, called **Avogadro Number**:

$$N_A \approx 6.02 \cdot 10^{23} \frac{1}{mol}$$

- **Molar Mass,  $\mu$  [g/mol]** is the mass of 1 mole of a given substance. To find it, you need to add up **atomic weights** of all the atoms in a single molecule. Those can be found in Periodic Table.

**Example:**

$$\mu_{H_2O} = (2 + 16) \frac{g}{mol} = 18 \frac{g}{mol}$$

	Volume	Mass	Amount of Substance	Number of Molecules
<b>Symbol</b>	<b>V</b>	<b>M</b>	<b>n</b>	<b>N</b>
<b>Units</b>	[m <sup>3</sup> ] or [cm <sup>3</sup> ]	[kg] or [g]	[mol]	<b>1</b>



$$\rho = \frac{M}{V}$$

Greek 'rho'

$$n = \frac{M}{\mu}$$

Greek 'mu'

$$V = \frac{N}{N_A}$$

# Ideal Gas Law (revisited)

Classical version (with moles)

$$PV = nRT$$

Here  $n = \frac{m}{\mu}$  is amount of substance (in moles),  
 $R \approx 8.3 \frac{J}{mol \cdot K}$  is called Universal Gas Constant.

“Molecular” version

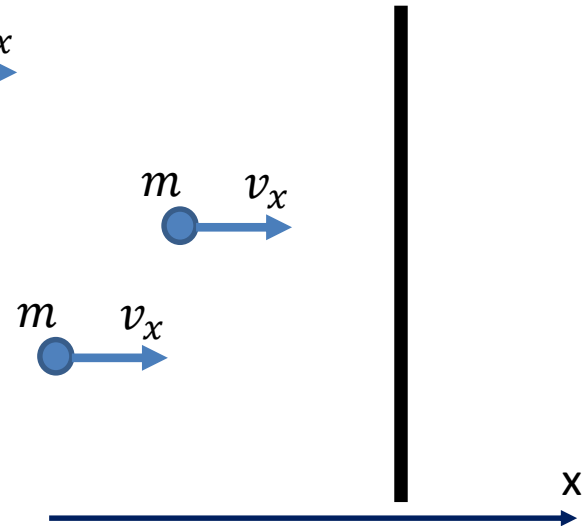
$$PV = Nk_bT$$

Here  $N = n \cdot N_A$  is number of molecules,  
 $k_B = \frac{R}{N_A} \approx 1.36 \cdot 10^{-23} \frac{J}{K}$   
is called Boltzmann Constant

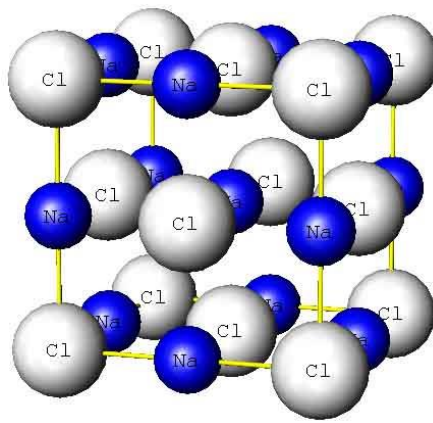
Kinetic energy per degree of freedom is

$$\frac{mv_x^2}{2} = \frac{k_bT}{2}$$

$$PV = Nm v_x^2$$



Results of Boltzmann's kinetic theory: pressure of molecules bombarding the wall.



### Problem 1

Table salt (or Sodium Chloride,  $NaCl$ ) is made of Sodium ( $Na^+$ ) and Chlorine ( $Cl^-$ ) ions held together by static electricity. Ions are atoms with extra or missing electrons (in this case, Chlorine steals one electron from Sodium). These ions form a cubic crystal as the one shown in the Figure. Find the distance ' $a$ ' between the centers neighboring ions ( $Na$  and  $Cl$ ), in cm, if the density of  $NaCl$  is  $\rho=2.16$  g/ml.

Hint: you already know how to find the number of  $Na$  and  $Cl$  ions in any volume, i.e.  $1\text{ ml}=1\text{ cm}^3$ . On the other hand, each ion occupies one cube of volume  $a^3$ .

### Problem 2

What is the number of molecules in a room of size  $4 \times 5 \times 2.5$  meters, at normal conditions ( $T=300\text{K}$ ,  $P=100\text{kPa}$ )? Find the total kinetic energy of these molecules, associated with motion in all three directions (i.e. account for 3 degrees of freedom per molecule, ignore rotation).

