

Positive and negative numbers. Absolute value of a number.

$$\begin{cases} |a| = a, & \text{if } a \geq 0 \\ |a| = -a, & \text{if } a < 0 \end{cases}$$

Complex fractions.

Complex fractions are formed by two fractional expressions, one on the top and the other one on the bottom, for example:

$$\frac{\frac{1}{2} + \frac{1}{3}}{\frac{7}{9} - \frac{2}{5}}$$

The fraction bar is a just another way to write the division sign, so we can re-write:

$$\frac{\frac{1}{2} + \frac{1}{3}}{\frac{7}{9} - \frac{2}{5}} = \left(\frac{1}{2} + \frac{1}{3}\right) \div \left(\frac{7}{9} - \frac{2}{5}\right)$$

It is easy to simplify a complex fraction:

$$\frac{\frac{1}{2} + \frac{1}{3}}{\frac{7}{9} - \frac{2}{5}} = \left(\frac{1}{2} + \frac{1}{3}\right) \div \left(\frac{7}{9} - \frac{2}{5}\right) = \frac{\frac{3}{6} + \frac{2}{6}}{\frac{35}{45} - \frac{8}{45}} = \frac{\frac{5}{6}}{\frac{27}{45}} = \frac{5}{6} \div \frac{27}{45} = \frac{5}{6} \cdot \frac{45}{27} = \frac{5}{1} \cdot \frac{2}{11} = \frac{10}{11}$$

GRAPHS

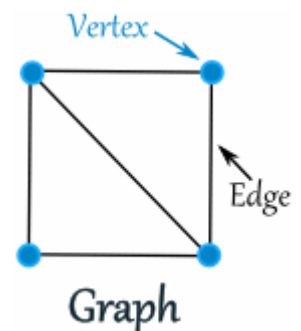
A graph (G) is a mathematical model consisting of a finite set of vertices (V) and a finite set of edges (E). The vertices, represented by points, may be connected by edges, represented by line segments.

Lines of the graphs- Segments

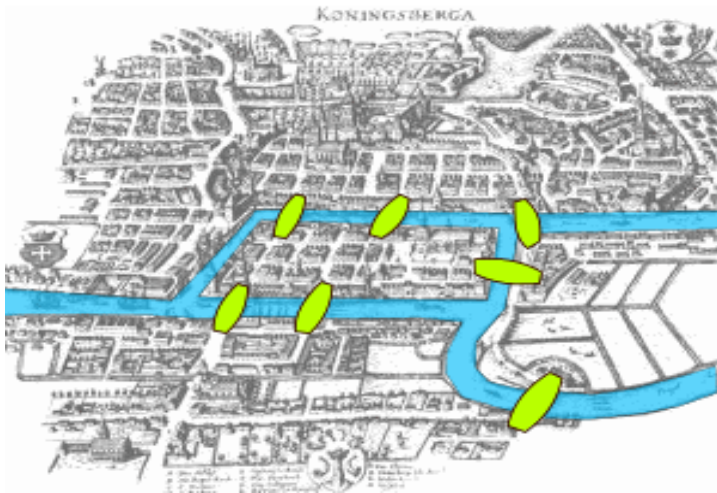
Points where segments intersect- VERTICES (“Vertex” in singular) or NODES

The number of segments originating from a vertex is called THE DEGREE OF THE VERTEX. In other words, the degree of a node is the number of edges touching it.

A vertex that has degree equal to zero is called an isolated vertex.

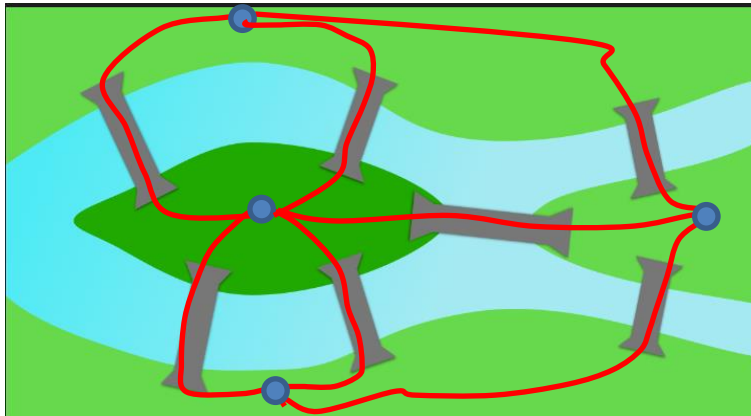


The old town of Königsberg has seven bridges:



Can you leave your home, take a walk through the town, visiting each part of the town and returning home crossing each bridge only once?

Euler (pronounced as [Oiler]) showed that the possibility of a walk through a graph, traversing each edge exactly once, depends on the degrees of the nodes.

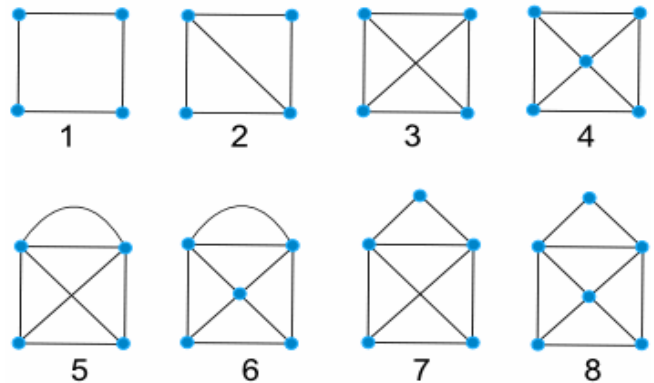


An Eulerian cycle, Eulerian **circuit** in a graph is a cycle that uses each edge exactly once and it ends in the vertex from which it started.

An Eulerian path uses each edge exactly once but it ends in a different vertex

A graph can be drawn with a single line if and ONLY if:

1. The graph is connected
2. The number of vertices with the odd degrees in the graph are 0 or 2



# of ODD Vertices	Implication (for a connected graph)
0	There is at least one Euler Circuit.
2	There is no Euler Circuit but at least 1 Euler Path.
more than 2	There are no Euler Circuits or Euler Paths.