## MATH 7 <br> QUADRATIC AND INEQUALITIES REVIEW

## Homework

1. (a) Find the minimal possible value of the expression $x^{2}+4 x+2$
(b) Given a number $a>0$, find the maximal possible value of $x(a-x)$ (the answer will depend on a).
2. What is the smallest possible value of $x^{2}+4$ ?
3. Find the value of $a$ for which the quadratic $a x^{2}-4 x+4=0$ has a double root.
4. Find all $x$ such that $2 x^{2}=1-x$
5. Factor $x^{4}-81$.
6. Graph: $f(x)=x^{2}+x-2$ and $g(x)=-x^{2}-x+2$
7. Solve the inequality: $|2-x|>3$. Use interval notation for your answer.
8. Use the snake method to solve the inequality: $x^{2}(x+1)(x-1)(x+2)>0$
9. Solve the equation $x^{2}-3 x-4=0$
10. Find $a, b, c$ for which $a x^{2}+b x+c=(2 x-1)(1-x)$.
11. Let $x_{1}, x_{2}$ be the roots of the equation $x^{2}-5 x+6=0$. Find
(a) $x_{1}^{2}+x_{2}^{2}$
(b) $\left(x_{1}-x_{2}\right)^{2}$
$\begin{array}{ll}\text { (c) } \frac{1}{x_{1}}+\frac{1}{x_{2}} & \text { (d) } x_{1}^{3}+x_{2}^{3}\end{array}$
(hint for part (d): compute first $\left(x_{1}+x_{2}\right)\left(x_{1}^{2}+x_{2}^{2}\right)$ )
