Math 5a, homework 13.

1. On a line mark two points. How many segments were formed? Add one there now? How many segments 6 points will form on the line? 10? 99?
2. 3 lines intersect at 1 point and form 6 angles. One is $44^{\circ}$, another is $38^{\circ}$. Can you find all other angles? Draw the picture. Use protractor and ruler.
3. The length of the segment $[\mathrm{MN}]=12 \mathrm{~cm}$. Point B divides the segment $[\mathrm{MN}]$ into two segments. Find the distance between the centers of these two segments. Explain your answer.
4. Draw Venn diagram for sets $\mathrm{A}, \mathrm{B}$, and C as on the picture. Shade the following areas;
a. $A \cap B$;
b. $A \cap C$;
c. $A \cup B$;
d. $A \cup C$;
e. $(A \cap B) \cup C$;
f. $A(\cup) \cap C$;
g. $(A \cap C) \cup(B \cap C)$

5. $\operatorname{Set} \mathrm{A}=\{2,5,6,8,12,19,24,32,45,47\}$.

Write subsets of the set A
a. of prime numbers
b. of composite numbers
c. divisors of 24
d. not multiples of 2
e. multiples of 3 and 5
f. multiples of 3 or multiples of 5
g. divisors of 8 or divisors of 12
h. divisors of 8 and 12 .
6. Simplify the following expressions (rewrite the expressions without parenthesis, combine like terms);

Example:

$$
(2 x+3) \cdot(x+7)=2 x x+2 x \cdot 7+3 x+3 \cdot 7=2 x^{2}+17 x+21
$$

a. $(x-1)(x+1)$;
b. $(a+1)(a+1)$;
c. $\quad(x+5)(x+y+3)$
d. $(k-1+d)(k-d)$;
e. $\frac{2}{3}+2 x\left(\frac{1}{2}-\frac{1}{3} y\right)-x-\frac{1}{3}(2-2 x y)$ f. $\quad 2 x^{2}(x+y)-3 x^{2}(x-y)$;
7. Sea water contains $5 \%$ salt (by weight). How many kilograms of fresh water should be added to 40 kg of sea water to obtain a solution with $2 \%$ salt?
8. Positive or negative value of $m$ will make the following equalities true statements?
$|m|=m$

$$
\begin{gathered}
m=-m \\
m+|m|=0 \\
m+|m|=2 m \\
m-|m|=2 m
\end{gathered}
$$




