Math 4a. Classwork 20.

## Ratio and percent.

1 percent of quantity is a $\frac{1}{100}$ th part of it.
$\mathbf{1 \%}$ of this line is shaded green: it is very small, isn't it?

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## Example 1.

To find $15 \%$ of 200 we need to divide 200 by 100 (how much is $1 \%$ ) and then multiply the result by 15 (how much is $15 \%$ ):

$$
\begin{gathered}
\frac{200}{100} \cdot 15=2 \cdot 15=30 \\
\frac{200}{100} \cdot 15=200 \cdot \frac{15}{100}=0.15 \cdot 200
\end{gathered}
$$

$15 \%$ is $\frac{15}{100}$ or 0.15 of a number (quantity).

## Example 2.

$7 \%$ of a number is 25 . What is the number?
We need to divide 25 by $8 \%$ (to know how much is $1 \%$ ) and multiply by 100 to find the number.

$$
\frac{25}{8} \cdot 100=25 \cdot \frac{100}{8}=25: \frac{8}{100}=25: 0.08
$$

## Example 3.

Fresh cranberries contain $90 \%$ of water, while dry cranberries contain only $15 \%$ of water. How much water should be evaporated from 4.25 kg . fresh cranberries to obtain dry cranberries?
To find out how much water is in 4.25 kg . of fresh cranberries we need to calculate:

$$
4250 \cdot 0.9=4250: 100 \cdot 90=3825 \mathrm{~g} .
$$

So, there are 3825 g . of water and 425 g . of fiber/sugar/vitamins and other minor components of cranberries. After drying process, 425 g of fiber/sugar/vitamins will still be in the berries, but some water will be evaporated, leaving only $15 \%$ of the final product as water. Therefore, we can tell that 425 g . of fiber/sugar/vitamins is constitute $85 \%$ of the final product, and $15 \%$ is water. To find the amount of water in the final product:

$$
425: 85 \cdot 15=75 \mathrm{~g} .
$$

The last step is:

$$
3825-75=3750 \mathrm{~g}
$$

During the process. 3750 g . of water should de evaporated.

## Exercises:

1. How many squares we have to shade to shade $10 \%$ of the line, $15 \%, 20 \%, 25 \%$ ?

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2. There are 200 pencils in the box. $3 \%$ of the pencils are red, $26 \%$ are yellow, and the rest are blue. How many red pencils are in the box?
3. Find:
a. $1 \%$ from 100
b. $7 \%$ from 200
c. $100 \%$ from 49
d. $1 \%$ from 300
e. $20 \%$ from 15
f. $120 \%$ from 250
g. $5 \%$ from 50
h. $25 \%$ from 48
i. $200 \%$ from 300
4. Find a number, if
a. $1 \%$ of it is 2 ;
b. $10 \%$ of it is 12 ;
c. $15 \%$ is 150 ;
d. $3 \%$ of it is 0.24 ;
e. $200 \%$ of it is 400 ;
f. $100 \%$ of it is 0.1 ;
g. $50 \%$ of it is 1 ;
h. $25 \%$ of it is 30 ;
5. $15 \%$ of the participant of math Olympiad solved 1 problem, $25 \%$ of the participant solved 2 problems, and the rest 24 students solved all three problems. Haw many students did participate in the math Olympiad?
6. Dry apricots contain $25 \%$ of water. How much water should be evaporated from 5 kg of fresh apricots to get dry apricots, if fresh apricots contain $85 \%$ of water?
7. Peter spent $15 \%$ of his money and 1.5 dollars on a doughnut and $\frac{3}{5}$ of his money and 30 cents on ice-cream. How much money did he have?
8. In Peter's bottle there is $10 \%$ more soda than in John's bottle. Peter drank $11 \%$ of his soda, while John drank $2 \%$ of his soda. So, who has more soda left?
9. Write an expression to find $15 \%$ of a number $\boldsymbol{a}$. Calculate $15 \%$ of the following numbers: 1540, 220, and 10 .
10.Write an expression to find a number, if $4 \%$ of it is equal to $\boldsymbol{b}$. Find the numbers for which $4 \%$ is equal to 8,12 , and 55 .
