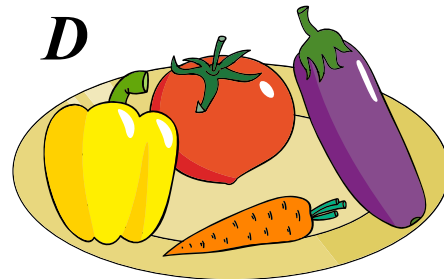
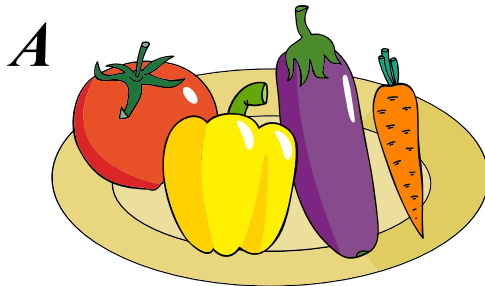


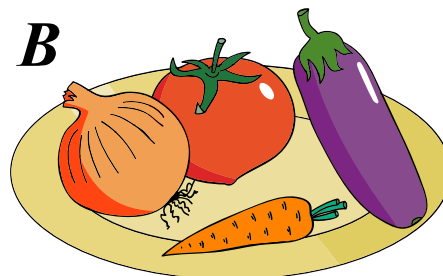
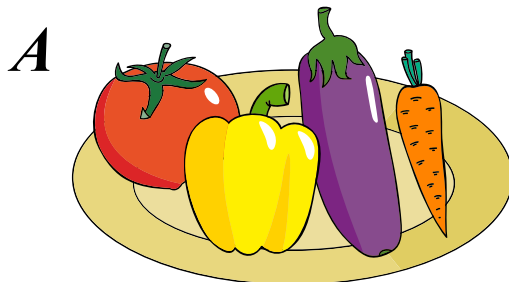
Lesson 4

1 Are the vegetables on plates *A* and *B* the same?



$A = D = \{ \underline{\hspace{2cm}}, \underline{\hspace{2cm}}, \underline{\hspace{2cm}}, \underline{\hspace{2cm}} \}$

Two sets are called **equal** if all their elements are the same.



Two sets are **not equal** if there is an element that belongs to one set but not to the other.

To write if two sets are equal or not, we use the signs “=” and “ \neq ”.

$A = \{ \underline{\hspace{2cm}}, \underline{\hspace{2cm}}, \underline{\hspace{2cm}}, \underline{\hspace{2cm}} \}$

$B = \{ \underline{\hspace{2cm}}, \underline{\hspace{2cm}}, \underline{\hspace{2cm}}, \underline{\hspace{2cm}} \}$

$A \neq B$

Which element belongs to set *A* but not to set *B*? _____

Which element belongs to set *B* but not to set *A*? _____

2 Check if the sets below are compared correctly:

a) $\{\text{♪}, \text{☺}, \text{◇}, \text{☀}, \text{♥}\} = \{\text{♪}, \text{◇}, \text{☺}, \text{♥}, \text{☀}\}$

b) $\{\text{♪}, \text{◇}, \text{☀}, \text{▲}, \text{♪}\} = \{\text{♪}, \text{♪}, \text{☺}, \text{♥}, \text{▲}\}$

c) $\{\#, \text{■}, \bullet, \circ, \text{☀}\} = \{\#, \text{■}, \bullet, \text{♪}, \text{☀}\}$

3 Let set $A = \{0, 1, 2\}$

State and explain which of the sets are equal to A :

$B = \{2, 0, 1\}$

$C = \{1, 0\}$

$D = \{3, 2, 1, 0\}$

A set without elements is called an **empty set**.

The symbol for an empty set is \emptyset .

4 Do you see any whales swimming inside your classroom? _____

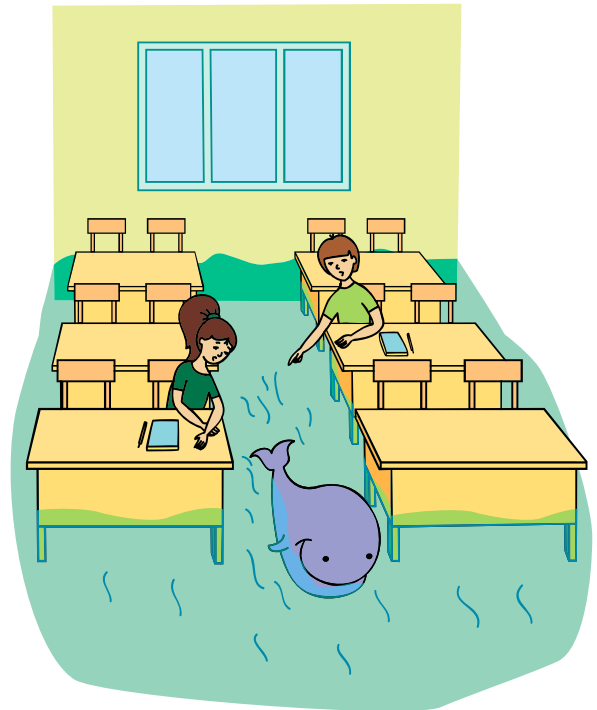
The set of whales swimming in your classroom is an empty set!

What do we call a set of six-legged horses? _____

What do we call a set of crocodiles living on the North Pole? _____

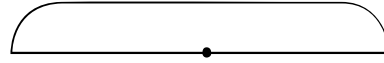
What do we call a set of 3 year olds in the third grade? _____

What other example of an empty set do you know? _____

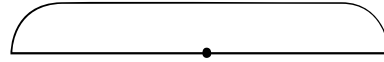


5 For each of the problems below, select the appropriate diagram to use and write the expressions.

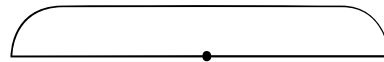
a) Nick saved x dollars for his sister's birthday. His brother Tom saved y dollars for the same occasion. How much money did the boys save together?



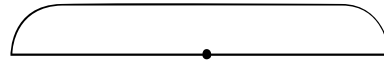
b) There are 5 eggs in each of n baskets. How many eggs are there in total?



c) Each month Lisa saves w dollars towards buying a new bike. She needs to keep saving for q months to purchase the bike. How much does it cost?

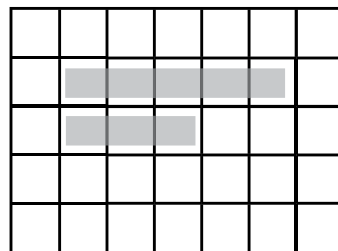


d) There are m books on each of q shelves. How many books are there on the shelves in total?



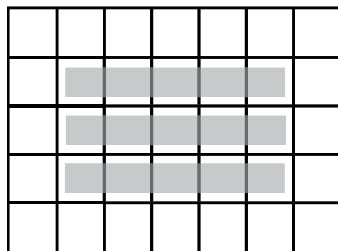
6 Fill in the tables:

	4	5	7	8
3 more				
3 times more				

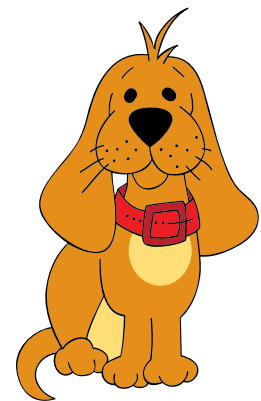


3 more

	4	5	7	8
5 more				
5 times more				



3 times more



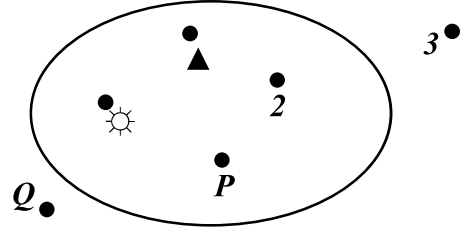
\times

$+$

Venn Diagram

7 Take a look at the diagram of a set A . List the elements that belong to the set A . Which elements do not belong to the set A ?

$A = \{ \quad , \quad , \quad , \quad \}$



_____ do not belong to set A .

Venn Diagrams are used to visualize sets:

any object within the oval belongs to the corresponding set;
any object outside the oval does not belong to the set.

The symbol \in means “belong”
The symbol \notin means “does not belong”

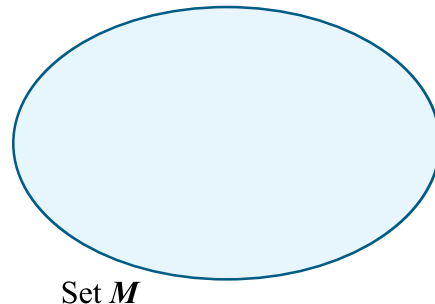
Examples:

$v \in K$
 $w \notin K$
 $2 \in K$
 $3 \notin K$

8 Set $M = \{a, \text{☀}, \text{♥}, 2, \text{♪}\}$

Complete statements with the symbols \in or \notin , and place the elements in the Venn Diagram accordingly:

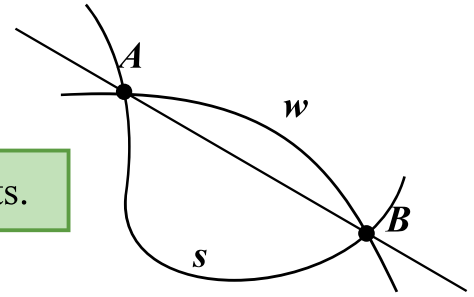
- | | |
|----------------------|----------------------|
| $a \square M$ | $\text{♪} \square M$ |
| $9 \square M$ | $\text{♥} \square M$ |
| $\text{☀} \square M$ | $5 \square M$ |
| $\text{☺} \square M$ | $2 \square M$ |



9 If you had to walk from point A to point B which path would you choose?

What is the shortest path from point B to point A ?

A straight line is the shortest path between any two points.



How many different straight lines can one plot through two points? _____

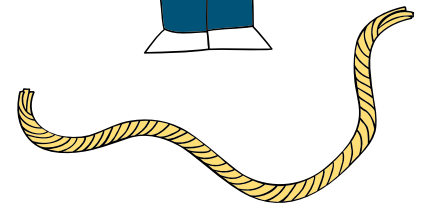
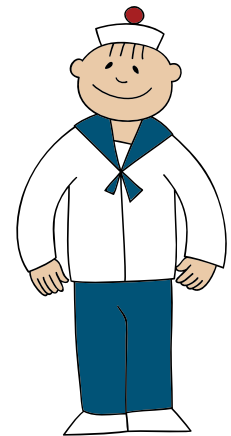
10 Draw two curved lines e and q between points A and B .

Find a point that belongs to the line e , but not to the line q . Mark it N .

How many different curved lines can one draw between points A and B ?

Draw the shortest path between points A and B .

A



B

11 Which of the statements about the diagram you drew are incorrect? Cross them out:

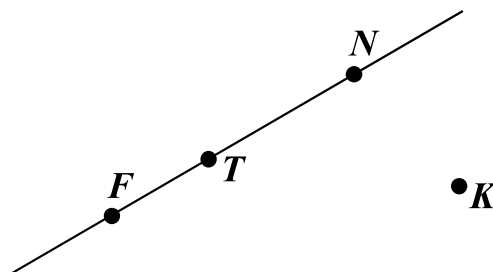
$A \in e$ $N \in e$ $N \notin e$ $A \in AB$ $A \notin q$ $e = q$ $q \neq e$

12 Look at the diagram and evaluate the statements as TRUE or FALSE. Cross out the false statements.

$F \in TN$ $N \in TF$

$TN = FN$ $NF \neq TF$

$K \in TN$ $TK = TN$



13 Curve e is a circle. Measure its radius and evaluate the statements as TRUE or FALSE:

$$e = \text{Circ}(N, 3 \text{ cm})$$

$$e = \text{Circ}(W, 4 \text{ cm})$$

$$e = \text{Circ}(W, 3 \text{ cm})$$

$$F \in e$$

$$W \in e$$

$$|WA| = 3 \text{ cm}$$

$$|WR| = 4 \text{ cm}$$

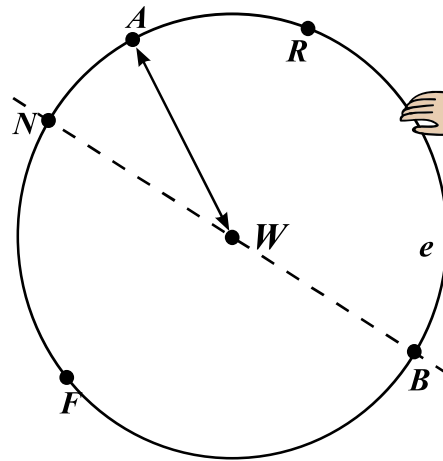
$$|NB| = 3 \text{ cm}$$

$$|NB| = 6 \text{ cm}$$

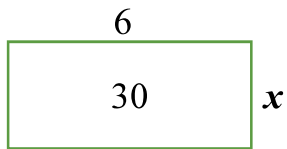
$$R \in e$$

$$|AR| > |NB|$$

$$|WR| = |WF|$$



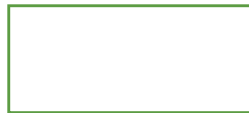
14 Use rectangles to visualize and solve the following equations:



$$x \times 6 = 30$$

$$x =$$

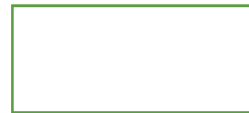
$$x =$$



$$42 \div y = 7$$

$$y =$$

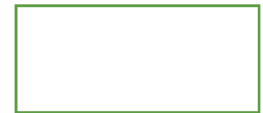
$$y =$$



$$9 \times z = 72$$

$$z =$$

$$z =$$



$$t \div 6 = 8$$

$$t =$$

$$t =$$

15 Do you remember Little Joe and Foxy Tail? Foxy Tail always lies and Little Joe always tells the truth.

FT: My brother LJ likes milk.

LJ: My brother FT likes milk

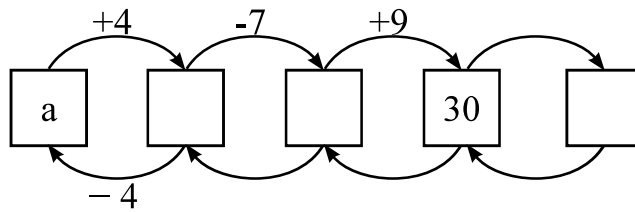
Which of the two brothers likes milk?



Equations with Multiple Operations

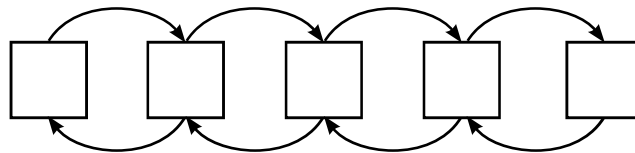
16 Analyze the listed in equations and undo the operations to find the unknowns.

$a + 4 - 7 + 9 = 30$
$a = 30 - 9 + 7 - 4$
$a =$
✓

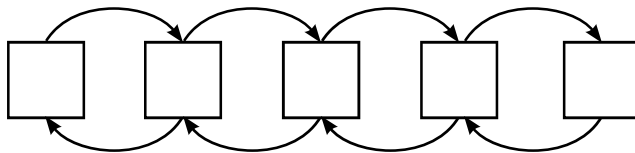


Operations are undone in reverse order.

$w - 7 - 12 = 9$
$w =$
$w =$
✓



$x - 8 + 11 - 4 = 9$
$x =$
$x =$
✓



17 Set $P = \{a, 2, 5, q, d, 4\}$

Place the following objects into the Venn Diagram:

$a, b, c, d, e, 1, 2, 3, 4, 5.$

