Homework 20.

Unlike simple mechanical systems, gases can not be practically characterized by coordinates and velocities of each molecule – there is just not possible to perform calculations over billions of billions of molecules. Instead we can pick up some average parameters such as temperature T, pressure P and volume V (volume here is the volume of jar or bottle where the gas is kept). Pressure is measured in N/m² (Pa), Volume in m³, Temperature in degrees according to Kelvin's scale (K). One Kelvin's degree equals to 1 Celsius degree, but zero at the Celsius scale is 273 degrees at the Kelvin's scale (or simply 273K). For example, room temperature is 27°C, but 300K.

For ideal gas (we call gas "ideal" if the molecules do not interact with each other -they do not attract or repulse) T,P and V are connected by a simple equation:

$$PV = nRT$$

where *n* is the number of molecules measured in *moles*, R is a constant which equals 8.31 J/(mole K), or 8.31×10^3 J/(kmole K). One mole is a certain *number* of atoms or molecules. If we take ~ 6×10^{23} molecules of, say, water we will have one mole of water (6.02×10^{23} is called Avogadro's number). 1 kilomole (kmole) = 1000 moles.

How to find the number of moles (or kmoles) if we know a mass of a substance? First we have to find a mass of one molecule of the substance. To do that, we need to take a look into the periodic table of elements.

Periodic table of elements

Chemical elements are the "building blocks" of nature. All the objects around us are "constructed" from chemical elements. Despite great variety of the objects and substances around us there are only 118 chemical elements (some of them are not shown in the table below). They are systematized and arranged in the table which is called periodic table of elements.

hydrogen 1	6.52				12	2		1	174			1000	251		157			bellum 2
H 1.0079 Ithium	beryflium											ī	boron	carbon	nitrogen	oxygen	fluorine	He 4.0026
³ Li	Be												B	ĉ	7 N	ů	° F	10 Ne
6,941	9.0122												10.811	12.011	14.007	15.999	18.998	20.180
södium 11	magnesium 12												aluminium 13	silicon 14	phosphorus 15	suffur 16	chiorine 17	argon 18
Na	Mg												AI	Si	P	S	CI	A
22.990 potassium	24.305 caldium	1	scandium	titanium	vanadium	chromium	manganese	iron	cobalt	nickel	copper	zine	26,982 galllum	28.086 germanium	30.974 arsenic	32.065 selenium	35.453 bromine	39.948 kryptor
19	20		21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
K	Ca		Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
39.098 rubidium	40.078 strontium	8	44.956 yttrium	47.867 zirconium	50.942 niobium	51,996 molybdenum	54.938 technetium	55.845 ruthenium	58.933 rhodium	58.693 palladium	63.546 silver	65,39 cadmium	69.723 Indium	72.61 tin	74.922 antimony	78.96 tellurium	79.904 kodine	83.80 xenon
37	38		39 V	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
Rb	Sr 87.62		T 88,906	Zr 91,224	Nb 92,906	Mo 95.94	Tc	Ru 101.07	Rh 102.91	Pd	Ag	Cd	114.82	Sn	Sb	127.60	126.90	Xe
caesium 55	barium 56	57-70	lutetium 71	hafnium 72	tantalum 73	tungsten 74	rhenium 75	osmum 76	iridium 77	platinum 78	gold 79	mercury 80	thallium 81	lead 82	bismuth 83	polonium 84	astatine 85	radon 86
Cs	Ba	*	Lu	Ĥf	Та	W	Re	Os	Îr	Pt	Au	Hg	ΤI	Pb	Bi	Po	At	Rr
132.91	137.33	0	174.97	178.49	180.95	183.84	186.21	190.23	192.22	195.08	196.97	200.59	204.38	207.2	208.98	1209	1210	[222]
francium 87	radium 88	89-102	lawrencium 103	rutherfordium 104	dubnium 105	seaborgium 106	bohrium 107	hassium 108	moitnerium 109	ununnilium 110	unununium 111	ununbium 112		ununquadium 114				
Fr	Ra	* *	Lr	Rf	Db	Sg	Bh	Hs	Mt	Uun	Uuu	Uub		Uuq				
[223]	[226]		[262]	[261]	[262]	[264]	[264]	[269]	[268]	[271]	[272]	[277]		[289]				
*!	ida		lanthanum 57	cerium 58	praseodymium 59	neodymium 60	promethium 61	samarlum 62	europium 63	gadolnium 64	terbium 65	dysprosium 66	holmium 67	erblum 68	thulium 69	ytterblum 70	I	
*Lanthanide series			La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb		
			138.91 actinium	140.12 thorium	140.91 protactinium	144.24 uranium	[145] neptunium	159.36 plutonium	151.96 americium	157.25 curium	158.93 berkelium	162.50 californium	164.93 einsteinium	167.26 fermium	168.93 mendelevium			
* * Actinide series			89	90	91	92	93	94	95	96	97	98	99	100	101	102		
			Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No		

Periodic table of elements.

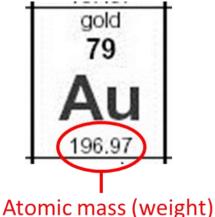
The periodic table was first suggested by a Russian chemist Dmitri Mendeleev in 1869. He found that if the chemical elements are arranged according their atomic mass, their chemical properties exhibit periodicity, that is why it is called "periodic".



Dmitri Mendeleev (1834-1907).

Only two of the chemical elements – mercury and bromine - are liquids at normal conditions (T=300K, atmospheric pressure), eleven elements are gases. The other elements are solids except nine elements (109-111 and 113-118) in the end of the table whose chemical properties are still unknown.

At the bottom of each cell of the table there is a number which represent the mass of the atom (atomic mass) in the so cold atomic units of mass.



One atomic unit of mass is 1.66×10^{-24} g, or 1.66×10^{-27} kg. It was chosen in such a way that if we take 1 mole of a substance (that means 6.02×10^{23} molecules), the mass of this 1 mole will be numerically equal to the atomic mass, but in grams.

For example, atomic mass of hydrogen (H) is ~1. A molecule of hydrogen consists of 2 atoms, so the mass of the molecule is 2 atomic units of mass. If we take 6.02×10^{23} molecules of hydrogen (1 mole), the total mass of the gas is 2g, or 0.002kg.

Another example: how many molecules (or moles) in 100g of water? A molecule of water consists of two atoms of hydrogen and one atom of oxygen. Let's look in the periodic table. Atomic mass of hydrogen is 1, atomic mass of oxygen is 16. So the mass of a molecule of water expressed in atomic units is 18. It means that a mass of 1 mole of water is 18g (we

can say that *molecular mass* of water is 18g). Now we can easily find how many moles in 100g of water: 100g:18g/mole~5.56moles. And we have total $5.56 \times 6.02 \times 10^{23} = 33.44 \times 10^{23} = 3.34 \times 10^{24}$.

Now, the problems (Please do not forget – we must use Kelvin's scale for temperature):

1. There is a 1 liter bottle filled with water at 27°C. The water is liquid at this temperature because there is attracting force between the molecules. Imagine, that we have suddenly "turned off" this attracting force. What is the pressure in the bottle now?

2. What is the volume of 1 mole of an ideal gas at the temperature of 27° C and pressure 105,000 N/m²?

3. This problem is a bit more challenging: find the formula which express the density of an ideal gas through its molecular mass (T= 27° C, P= $105,000 \text{ N/m}^2$).