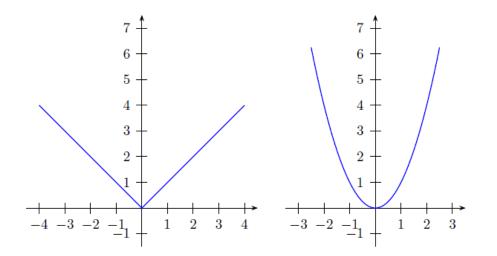
Math 6a/b: Homework 14 Homework #14 is due January 27.

## Graphs

Generally, a graph of function y = f(x) is some line in the x - y plane. If one has two graphs y = f(x) and y = g(x) one can find intersection points of corresponding graphs by solving the system of equations. For example, the intersection point of two straight lines y = x+2 and y = -x is the point (-1, 1) as x = -1 and y = 1 satisfy both of these equations; that is the point (-1, 1) lies simultaneously on both straight lines.

Graphs of y = |x| and  $y = x^2$ 

The figures below show graphs of functions y = |x| and  $y = x^2$ ; the latter graph is called a *parabola*.



And here is what we can do to draw a graph of any parabola of the *standard form*  $y = ax^2 + bx + c$ . You can verify the following identity yourself:

$$ax^{2} + bx + c = a(x - h)^{2} + k$$
 (vertex form), where  $h = -\frac{b}{2a}h$  and  $k = -\frac{b^{2}-4ac}{4a}$ .

You can <u>convert from standard to the vertex</u> form by using the coefficients *a*, *b*, *c* to obtain *h* and *k*, and then re-write the graph equation into the vertex form. For example:  $y = x^2 + x$  can be converted into  $y = (x + \frac{1}{2})^2 - \frac{1}{4}$ 

The result will be a parabola obtained by stretching the usual parabola vertically by factor a (if a < 0, this means flipping it upside down and then stretching by |a|) and then moving it so that the vertex will be at point (h, k). In particular, the branches go up if a > 0 and down if a < 0.

Obviously, the parabola either intersects y = 0 (x-axis) at two points, does not intersect it, or touches y = 0 at a single point. Correspondingly, the quadratic equation has two **roots**, no roots or one root respectively. One can easily check that this corresponds to D > 0, D < 0 and D = 0 respectively, where  $D = b^2 - 4ac$ .

## Homework

- 1. Find the equation of the line which passes through point (3,4) and has a slope +2. (Hint: you only need to find the intercept and write y = ax+b)
- 2. Find the equation of the line through points (-2, 0) and (0,2).
- 3. Sketch the graph of the functions: y = |x + 1| and y = -x + 0.25. How many solutions do you think the following equation has?

$$|x+1| = -x + 0.25$$

Note: you are not asked to solve the equation – just answer how many solutions there are.

- 4. Find the intersection point of a line  $y = \frac{1}{4}x^2$  and a line y = 2x+1. Sketch or draw the graphs. (Hint: construct a system of equations and solve).
- 5. Sketch/draw graphs of the following functions: a) x + y = 2b) y = |x - 5| + 1c) y = |x + 1| + |x - 2|d) y = |x + 1| + |x + 2| + |x + 3|
- 6. Sketch/draw graphs of the following function:  $y = -x^2 + 4x 3$ 
  - a) To sketch, convert the function from standard to vertex form and use your knowledge of what a, h, and k mean.
  - b) If you cannot convert to vertex form, select points for x, then calculate the corresponding y-values as you will do to graph any other function.
  - c) Does the graph intersect the y = 0 line (x-axis) these are known as **roots**.
  - d) Does the number of roots correspond to the D-value? (\*optional)