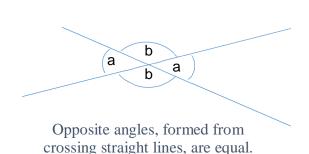
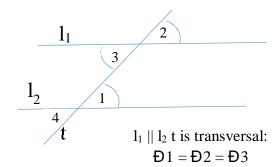
Geometry: parallel lines, parallelogram





$$\mathbf{D} \mathbf{a} = \mathbf{D} \mathbf{a} - \mathbf{opposite}$$

 Θ a + Θ b = 180 ⁰ – on a straight line,

Or complementary angles

D1 = D3 = alternate interior angles

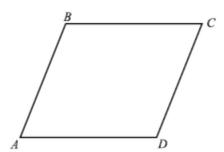
D1 = D2 =corresponding angles

 $\mathbf{D}4 = \mathbf{D}2 = \text{alternate exterior angles}$

Theorem 1: If two parallel lines (11 and 12) are intersected by a third line (t), then the formed alternate interior angles are equal.

Theorem 2: If two alternate interior angles formed when two lines (11 and 11) crossed by a third (t) are equal ($\Theta 1 = \Theta 3$), then the two lines (11 and 12) are parallel.

Parallelogram: A parallelogram is a quadrilateral in which opposite sides are parallel. Parallelograms have a number of interesting properties, which we will study later.

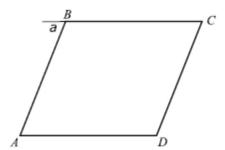


Sum of angles of an n-gon

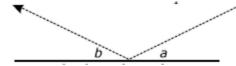
Recall that sum of angles of a triangle is 180° . Since a quadrilateral can be cut into 2 triangles, sum of angles of a quadrilateral is $2 \times 180^{\circ} = 360^{\circ}$. Similarly, for a pentagon we get $3 \times 180^{\circ}$, and for an n-gon, the sum of angles is $(n - 2) \times 180^{\circ}$.

Homework

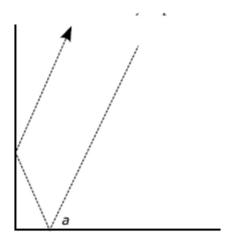
- 1. Is it true that any rectangle is also a parallelogram? Is it true that any parallelogram is a rectangle? Try to argue as carefully as you can.
- 2. Show that in a parallelogram, diagonally opposite angles are equal $\Theta A = \Theta C$, $\Theta B = \Theta D$ [Hint: see figure below, we did this in class, try to repeat the arguments]



- 3. Show that the previous problem also works in the other direction: if in a quadrilateral, diagonally opposite angles are equal: $\Theta A = \Theta C$, $\Theta B = \Theta D$, then the quadrilateral must be a parallelogram.
- 4. Cut two identical paper triangles (the easiest way to do it is to fold a sheet of paper in two and then cut). Can you put these two triangles together so that they form a parallelogram? Will your method always work? Why?
- 5. Antonia and Gabi took a 9-mile trip in a rowboat. There was only one pair of oars, so they took turns rowing (however, they didn't time how long each of them was rowing, so it could happen that one had rowed longer than the other). Antonia could row at the speed of 3 miles per hour; Gabi could only do 2 miles per hour. It took them 3.5 hours to complete the trip. Can you find out how long each of them was rowing?
- 6. An n-gon is called regular if all sides are equal and all angles are also equal.
 - (a) How large is each angle in a regular hexagon (6-gon)?
 - (b) How large is each angle in a regular heptagon (7-gon)?
- 7. The reflection law states that the angles formed by the incoming light ray and the reflected one with the surface of the mirror are equal: $\Theta a = \Theta b$



Using this law, show that a corner made of two perpendicular mirrors will reflect any light ray exactly back: the reflected ray is parallel to the incoming one.



[Hint: find the angle which each of these lines form with the horizontal] This property – or rather, similar property of corners in three dimensions — is widely used: reflecting road signs, tail lights of a car, reflecting strips on clothing are all constructed out of many small reflecting corners so that they reflect the light of a car headlamp exactly back to the car.