## Review of Homework \# 21

1. Compute the value of the expressions $9 a^{2},(9 a)^{2},-9 a^{2},(-9 a)^{2}$ if :
a) $a=\frac{1}{6}$
b) $a=-0.1$
2. Rewrite the following expression without parenthesis:
$\left(\frac{1}{2}+a\right)(2+a)=$
$(n-a)(n+a)=$
$(a+b)(a+b)=(a+b)^{2}=$
$(2 a+2 b)(b-c)=$
3. I have 15 new books to choose from.
A) I have a 5-day vacation and I want to read 1 book every day. How many possible ways are there for me to read these 5 books?
B) I have a 3-day long vacation and I want to read 1 book every day. How many possible ways are there for me to read these 3 books?
4. Compute:
a. $\left(-\frac{1}{2}\right)^{5}$
b. $\left(-\frac{2}{3}\right)^{4}$
c. $\left(-\frac{4}{5}\right)^{3}$
1) Rewrite the following expressions without parenthesis:
a) $-3.64-(12.45-3.64)=$
b) $1 \frac{3}{8}+\left(-2 \frac{7}{9}+\frac{5}{8}\right)=$
c) $(5.6-7.2)-(-7.2+3.4)=$
d) $\left(2.4-\frac{2}{3}\right)+2.4-\left(1.8+1 \frac{5}{6}\right)=$
e) $45-(-7+18)-(34-18+26)=$
f) $-9.7+(-3.8+5.2)-(2.9-5.2-9.7)+3.8$
g) $-(a-b)$
h) $-(c+d)$
i) $-(-x+y)$
j) $d-(-k+t)$
k) $-m+(a-c)$

## 1. Equalities: equations and identities Inequalities.

An equation is the problem of finding values of some variables, called unknowns, for which the specified equality is true. To find the value of the unknown variable you must solve the equation. There are another kind of mathematical statements - inequalities.

Which $a$ can satisfy the statement: $a>2$ ?
As we can see all $a$ which lie on the right side of
 number 2 will satisfy the expression $a>2$. What about number 2 itself? Number 2 does not satisfy our expression. How we can wright the answer for $a>2$ ?

The best way to write the answer in terms of set theory: $a \in] 2, \infty)(a \in(2, \infty)$ ), or the answer is set of points of number line located on the right side of number 2.

- Now let's solve the inequality $a \geq 2$.

In this case number 2 itself also belongs to the set of numbers satisfying to our inequality and the answer will be $a \in[2, \infty)$


Can you find all $x$ satisfying two following inequalities at the same time: $\quad x \geq-1$ and $x<5$ ?
Write the set X containing all whole numbers satisfying these two inequalities at the same time?
The answer is :

| -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

We can add any number to both part of the inequality, the sign ( $<$ or $>$ ) will not change:
$x>-1$

| -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -4 | 1 | - | -1 | 0 | 1 | 2 | 3 | 4 |
| -4 | -3 | -2 | -1 | 1 |  | 2 |  |  |

$x+2>-1+2 \Rightarrow x+2>1$
$y-3<5$
$y-3+3<5+3$

$y<8$,
$y \in(-\infty, 8)$

Now let's try to multiply or divide both part of the inequality by the positive number. If $x>3$, then $2 x$ will be grater then 6 .

$x>3, \quad 2 x>6$
$-2 x>6$
When you multiply or divide each side of an inequality by a negative numberyou have to swap the inequality:
$1<2 \quad-1 \times 1>-1 \times 2$

$$
\text { 1. } x+3>5 x-5
$$

2. $4 x-3 \neq 0$
3. $3(x-1)<5 x+9$
4. $2 x-1>-x+3$
5. $|x|>8$

- I want to spend less than a $150 \$$ on the gifts for my 25 students. Write an inequality to represent the price I want to pay per each gift


## Geometry: Median, Height, Bisector



- A median of a triangle is a segment that connects any vertex of the triangle with the mid-point of its opposite side
- A median of a triangle divides the triangle into two equal areas

- The point where all three medians of a triangle intersect called 'centroid'


The Bisector of an angle is a ray whose end point is the vertex of the angle and which splits the angle onto two equal angles.

How to construct angles and various geometrical figures:
https://www.mathopenref.com/tocs/constructionstoc.html
In the diagram to the right, the ray CD is the
bisector of the angle ACB if and only if the angles
ACD and BCD have equal measures.

## How to construct an angle bisector:

John D. "Math Open Reference" www.mathopenref.com

You are given an angle. Let's call it ABC.


Step 2. Draw two more arcs. The first arc must be centered on one of the two points $\mathbf{P}$ or $\mathbf{Q}$. It can have any length radius. The second arc must be centered on whichever point ( P or Q ) you did NOT choose for the first arc. The radius for the second arc MUST be the same as the first arc. Make sure you make the arcs long enough so that these two arcs intersect in at least one point. Let's call this intersection point $\mathbf{X}$. Every intersection point between these arcs (there can be at most 2) will lie on the angle bisector.

Step 3. Draw a line that contains both the vertex and $\mathbf{X}$. Since the intersection points and the vertex all lie on the angle bisector, we know that the line which passes through these points must be the angle bisector.


A video tutorial and printable instructions on how to construct an altitude of a triangle:
https://www.mathopenref.com/constaltitude.html
https://www.mathopenref.com/printaltitude.html

A video tutorial and printable instructions on how to construct a median of a triangle:

## https://www.mathopenref.com/constmedian.html

https://www.mathopenref.com/printmedian.html

